

# Contaminant source and aquifer characterization: An application of ES-MDA demonstrating the assimilation of geophysical data

Zi Chen<sup>a,b</sup>, Leli Zong<sup>a</sup>, J. Jaime Gómez-Hernández<sup>d</sup>, Teng Xu<sup>c,\*</sup>, Yuehua Jiang<sup>a,b</sup>,  
Quanping Zhou<sup>a,b</sup>, Hai Yang<sup>a,b</sup>, Zhengyang Jia<sup>a,b</sup>, Shijia Mei<sup>a,b</sup>

<sup>a</sup>*Nanjing Center, China Geological Survey, Nanjing, China*

<sup>b</sup>*Key Laboratory of Watershed Eco-Geological Processes, Ministry of Natural Resources, Nanjing, China*

<sup>c</sup>*College of Water Conservancy and Hydropower Engineering, Hohai University, Nanjing, China*

<sup>d</sup>*Institute of Water and Environmental Engineering, Universitat Politècnica de València, Valencia, Spain*

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## Abstract

Contaminant source and aquifer characterization (CSAC) is critical in groundwater pollution evaluation and remediation. The ensemble smoother with multiple data assimilation (ES-MDA) is utilized to jointly identify contaminant source information and hydraulic conductivities by assimilating time-lapse electrical resistivity tomography (ERT) data. In a synthetic profile with a time-varying release history in a heterogenous aquifer, we verify the performance of the proposed data assimilation framework. The results show that the CSAC problem could be handled by the proposed approach. The time-varying release history and the high permeability area can be identified with adequate time-lapse ERT measurements. Further reproduction of the evolution of the plume after CSAC also shows consistency with the reference plume. The poor conditioning inversion caused by the filter inbreeding is analyzed by comparing four scenarios with different apparent resistivity measurements. Furthermore, we also evaluate the impact of uncertainties in the petrophysical properties and geophysical observations on our data assimilation framework. The results show that the proposed ES-MDA data assimilation framework could provide a convincing inversion of the time-varying release history and hydraulic conductivities.

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\*Corresponding author

*Email address:* [teng.xu@hhu.edu.cn](mailto:teng.xu@hhu.edu.cn) (Teng Xu )

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## 1. Introduction

Groundwater is a fundamental component of the hydrologic cycle, crucial for water supply and with many dependent ecosystems. Unfortunately, they can be easily polluted by anthropogenic activities, such as landfill operations, industry leakages, urban sewage, and others. Groundwater contamination is an important issue that has drawn the attention of researchers in the past decades (Gómez-Hernández and Wen, 1994; Gómez-Hernández et al., 2003; Feyen et al., 2003; Li et al., 2011a,b; Megdal, 2018). A critical issue in groundwater contamination is the identification of the source of contamination together with the characterization of aquifer properties, mainly hydraulic conductivity. Inverse problems in hydrogeology have been the focus of many researchers, who have found it to be an ill-posed problem with different solutions (Carrera and Neuman, 1986; Capilla et al., 1998, 1999; Wen et al., 1999; Franssen and Gómez-Hernández, 2002; Bagtzoglou and Atmadja, 2005; Hanea et al., 2015).

To date, several methods have been developed for contaminant source identification and there are several good reviews available (Atmadja and Bagtzoglou, 2001; Michalak and Kitanidis, 2004; Gómez-Hernández and Xu, 2021). The methods summarized in these reviews could be classified into three main categories: optimization, probabilistic, and backward-in-time simulation methods. The optimization approaches build an objective function and attempt to minimize the discrepancies between simulated and observed measurements (Gorelick et al., 1983; Sun et al., 2006; Mirghani et al., 2009; Ayvaz, 2010; Li et al., 2012); the probabilistic approaches handle the problem with a stochastic framework and try to approximate the posterior probabilities of the simulated measurements conditioned on the observed ones (Woodbury and Ulrych, 1996; Zeng et al., 2012; Butera et al., 2013; Cupola et al.,

24 2015; Pirot et al., 2019; Jiang et al., 2021); backward-in-time simulation methods solve the  
25 solute transport equations backward to identify the most likely contaminant release loca-  
26 tions (Bagtzoglou et al., 1992; Neupauer and Wilson, 1999; Bagtzoglou and Atmadja, 2003;  
27 Ababou et al., 2010).

28 For the past few years, data assimilation methods have become increasingly prominent  
29 for their versatile and efficient features. The ensemble Kalman filter (EnKF) proposed by  
30 Evensen (2003) and the ensemble smoother with multiple data assimilation (ES-MDA) pro-  
31 posed by Emerick and Reynolds (2013) have been progressively employed for contaminant  
32 source identification. Xu and Gómez-Hernández (2016) first proposed the restart normal-  
33 score EnKF to handle the contaminant source identification problem and then extended this  
34 method to recognize contaminant source information and heterogeneous hydraulic conduc-  
35 tivity jointly (Xu and Gómez-Hernández, 2018). Li et al. (2019) employed a mixed integer  
36 nonlinear programming optimization model together with Kalman filter to deduce contam-  
37 inant source information. Panjehfouladgaran and Rajabi (2022) combined artificial neural  
38 networks and constrained the restart EnKF to characterize the pollutant source in a coastal  
39 aquifer and then moved one step further to identify aquifer heterogeneity in a tide-influenced  
40 coastal aquifer (Dodangeh et al., 2022). The ES-MDA method has been coupled with genera-  
41 tive adversarial networks by Bao et al. (2020) to handle a channelized aquifer characterization  
42 problem. Todaro et al. (2021) applied the ES-MDA method to recognize pollutant source  
43 location and release history. Furthermore, Xu et al. (2022) handled the non-point source  
44 identification puzzle via ES-MDA.

45 The aforementioned research findings are proof of the capacity of data assimilation meth-  
46 ods for the joint identification of pollutant sources and aquifer heterogeneity, however, despite  
47 a few applications in sandbox experiments, there is still a lack of verification in field cases.  
48 One main reason is that the measurements required are not available; at most, only a few  
49 sparse and discontinuous pollution data are accessible. One possible solution to the lack of

50 contaminant data could be the use of geophysical surveys. Geophysical methods have been  
51 extensively utilized in groundwater contamination investigation, especially electrical resistivity tomography (ERT), which is a cost-efficient and non-intrusive method with a high  
52 sampling density (Nenna et al., 2011; Seferou et al., 2013; Binley et al., 2015; Mao et al.,  
53 2016; Shao et al., 2021; Xia et al., 2021). ERT could be the perfect data source for ensemble-  
54 based contaminant source identification problems. As far as we know, several works have  
55 already combined data assimilation methods with ERT data to study groundwater movement  
56 or contamination issues. Crestani et al. (2013) first compared the ensemble Kalman filter  
57 (EnKF) and the ensemble smoother (ES) capabilities in identifying hydraulic conductivity  
58 via a tracer test, and then directly using the ERT data to inverse the heterogenous hydraulic  
59 conductivity in both a synthetic and a real test case (Crestani et al., 2015). Bouzaglou  
60 et al. (2018) combined the EnKF method and the SUTRA model to update groundwater  
61 states and soil parameters by using ERT measurements in a seawater intrusion laboratory  
62 experiment. Kang et al. (2018) first developed an EnKF-based data assimilation algorithm  
63 to jointly recognize DNAPL saturation together with a hydraulic conductivity field by as-  
64 simulating time-lapse ERT data and later employed the ensemble smoother-direct sampling  
65 method (ES-DS) to identify a non-Gaussian aquifer by using both time-lapse geophysical  
66 and geochemical datasets (Kang et al., 2019). Tso et al. (2020) utilised cross-borehole time-  
67 lapse ERT data to identify contaminant source information through an ensemble-based data  
68 assimilation framework. The aforementioned study substantiates the efficacy and depend-  
69 ability of the ERT technique when applied to the examination of groundwater contamination  
70 problems. However, the majority of these studies confine their focus solely to the identifi-  
71 cation of heterogenous hydraulic conductivity or contaminant source information, assuming  
72 the other factor is already known. These assumptions present significant impracticality when  
73 applied to real-world scenarios, owing to the inherent scarcity of subsurface information and  
74 the persistent lack of data to detect groundwater pollution.  
75

76 In this paper, we establish a benchmark that employs the ensemble smoother with multi-  
77 ple data assimilations (ES-MDA) to jointly identify time-varying release history and aquifer  
78 heterogeneity by using time-lapse ERT data. Besides, we also evaluate the impact of different  
79 cross-hole configurations on the proposed data assimilation framework. To our knowledge,  
80 this is the first instance of time-lapse ERT measurements being used for the joint identifica-  
81 tion of contaminant source information and hydraulic conductivities. The rest of this paper  
82 is organized as follows: First, we outline the methodology of the proposed data assimilation  
83 framework in section 2, including the coupling of groundwater flow, solute transport, and  
84 geophysical modeling into the ES-MDA implementation; then, in sections 3, a benchmark  
85 case with a time-varying releasing history in a heterogenous aquifer property is built that  
86 will be used as the reference to test the proposed method; section 4 evaluates the proposed  
87 approach, and follows a discussion in section 5; finally, in section 6, we summarize the main  
88 findings of this work and propose some future works need to be done.

## 89 2. Methodology

### 90 2.1. Groundwater flow and solute transport model

91 Groundwater flow and solute transport in an aquifer can be described by the following  
92 partial differential equations (Bear, 1972; Zheng and Wang, 1999)

$$93 \quad \nabla \cdot (K \nabla h) + w = 0, \quad (1)$$

$$94 \quad \frac{\partial (\theta C)}{\partial t} = \nabla \cdot (\theta D \cdot \nabla C) - \nabla \cdot (\theta v C) - q_s C_s, \quad (2)$$

96 where  $K$  represents hydraulic conductivity [ $LT^{-1}$ ];  $h$  stands for hydraulic head [ $L$ ];  $\nabla \cdot$  and  
97  $\nabla$  are the divergence and gradient operators, respectively;  $w$  stands for additional sources  
98 and sinks [ $T^{-1}$ ];  $C$  denotes the dissolved contaminant concentration [ $ML^{-3}$ ];  $\theta$  represents  
99 effective porosity of the medium [-];  $t$  denotes time [ $T$ ];  $D$  is a hydrodynamic dispersion

100 coefficient tensor [ $L^2T^{-1}$ ];  $v$  stands for the flow velocity of the groundwater [ $LT^{-1}$ ] obtained  
 101 from the solution of groundwater flow model (Eq. (1));  $q_s$  denotes the volumetric flow rate  
 102 per unit volume of aquifer associated with a fluid source or sink [ $T^{-1}$ ], while  $C_s$  stands for  
 103 the concentration of the source or sink [ $ML^{-3}$ ]. The solution of both equations requires  
 104 the specification of initial and boundary conditions. In this work, the groundwater flow  
 105 equation is numerically solved through the finite difference MODFLOW program (Harbaugh,  
 106 2005) while the solute transport equation is handled by the finite difference MT3D program  
 107 (Bedekar et al., 2016).

## 108 2.2. Geophysical model

109 The electrical potential field induced by a couple of electrodes can be characterized by  
 110 the following equation

$$111 \quad -\nabla \cdot \frac{1}{\rho} \nabla V = I(\delta(\mathbf{r} - \mathbf{r}_+) - \delta(\mathbf{r} - \mathbf{r}_-)), \quad (3)$$

112 where  $\rho$  is porous media resistivity;  $V$  denotes electrical potential field;  $I$  is the input current  
 113 from a dipole;  $\mathbf{r}_+$  and  $\mathbf{r}_-$  are the locations of the positive and negative electrodes, respectively,  
 114 and  $\delta(\cdot)$  is the Dirac delta function.

115 Here, the porous media resistivity depends on several factors, such as porosity or pore  
 116 water conductivity. The resistivity model proposed by Revil et al. (2018) is employed in this  
 117 work

$$118 \quad \frac{1}{\rho} = (S_w \phi)^m \sigma_w + (S_w \phi)^{m-1} \rho_s (B - \lambda) CEC, \quad (4)$$

119 where  $S_w$  is water saturation, which equals 1 in aquifers;  $\phi$  is porosity, which in this study  
 120 is 0.32 for both the coarse and fine sands (Power et al., 2013);  $m$  is a cementation exponent;  
 121  $\rho_s$  is grain density;  $B$  and  $\lambda$  are apparent mobility of the counterions responsible for surface

122 conduction and polarization, respectively;  $CEC$  is the quantity of exchangeable cation on  
 123 the surface of the silica grains, and can be calculated by the following equation (Revil, 2013;  
 124 Revil et al., 2017)

$$125 \quad CEC = 6 \frac{Q_s}{\rho_s d}, \quad (5)$$

126 where  $Q_s$  equals  $0.64 \text{ Cm}^{-2}$ ;  $d$  stands for the mean grain diameter of the sand.  $\sigma_w$  is  
 127 the conductivity of the pore water, which is determined by the ionic concentration and  
 128 temperature (Sen, 1992) according to the following expression

$$129 \quad \sigma_w = (5.6 + 0.27T - 1.5 \times 10^{-4}T^2)C - \left(\frac{2.36 + 0.099T}{1.0 + 0.214C}\right)C^{\frac{2}{3}}, \quad (6)$$

130 where  $T$  is temperature, which is assumed constant at  $25 \text{ }^\circ\text{C}$  in this research; and  $C$  is ionic  
 131 concentration.

132 In the context of resistivity field surveys, the apparent resistivity ( $\rho_a$ ) is preferred over  
 133 the resistivity as it serves as a proxy for the alteration in the electrical characteristics of the  
 134 subsurface medium with a specific electrode array configuration, defined by

$$135 \quad \rho_a = K \frac{\Delta U}{I}, \quad (7)$$

136 where  $K$  denotes a geometric factor which depends on the electrode array configuration;  $\Delta U$   
 137 stands for the potential difference between the two potential electrodes M and N.

138 Specifically, the apparent resistivity can be computed from the resistivity values obtained  
 139 from Eq. (4) by solving a geophysical forward problem. In this work, the geophysical forward  
 140 problem is solved by the finite-element open-source software ResIPy (Blanchy et al., 2020).

141 With the contaminant concentration calculated from MODFLOW and MT3DS and sev-  
 142 eral geophysical parameters, the resistivity values of the aquifer could be obtained from

143 Eq. (4),(5) and (6). Thus, with the geophysical forward model ResIPy, the relationship  
144 between apparent resistivity  $\rho_a$  and concentration  $C$  can be established.

### 145 2.3. Ensemble Smoother with Multiple Data Assimilation (ES-MDA)

146 The ES-MDA technology is employed to identify a contaminant source and aquifer het-  
147 erogeneity from apparent resistivity data. A short description of the ES-MDA is provided  
148 next, for a more in-depth discussion the reader is referred to Emerick and Reynolds (2013):

#### 149 1. Procedure

150 The first step of the ES-MDA technology is to generate a certain number  $N_e$  of realizations  
151 with unknown contaminant source and aquifer characterization (CSAC) parameters, which  
152 include time-varying release history and hydraulic conductivity spatial distribution in this  
153 work. Once the number of iterations  $N_a$  and the inflation factor  $\alpha_j$  (explained in detail below)  
154 are determined, the method will go through two main steps: forecast step and analysis step.

155 In the forecast step, for each member of the realizations, the groundwater flow, solute  
156 transport and geophysical models (MODFLOW, MT3DS and ResIPy) are solved sequen-  
157 tially,

$$158 \quad B_{i,j}^f = \psi[B_0, A_{i,j}], \quad (8)$$

159 where  $B^f$  denotes the vector of forecasted apparent resistivity, while  $B_0$  represents the vector  
160 of initial apparent resistivity;  $i$  stands for the realization index,  $i = 1, 2, \dots, N_e$  and  $j$  is the  
161 iteration index of ES-MDA,  $j = 1, 2, \dots, N_a$ ;  $\psi$  denotes the forward numerical simulators,  
162 which are MODFLOW, MT3DS and ResIPy in this case;  $A$  stands for the vector of CSAC  
163 parameters, including time-varying release history and hydraulic conductivity distribution.

164 Then, the CSAC parameters are updated using a truncated singular value decomposition



165 (TSVD) algorithm in the analysis step, the detailed procedure can be expressed as following,

$$166 \quad A_{i,j+1} = A_{i,j} + \Delta A_j (\Delta B_j^f)^T [\Delta B_j^f (\Delta B_j^f)^T + \alpha_j R]^{-1} [y_{obs} + \sqrt{\alpha_j} \varepsilon - B_{o,i,j}^f], \quad (9)$$

167 where  $i$  and  $j$  stand for the same meaning as in Eq. 8;  $\alpha_j$  stands for the inflation factor;  $y_{obs}$   
 168 denotes an  $N_o \cdot N_t \times 1$  vector of apparent resistivity observations ( $N_o$  denotes the amount  
 169 of measurements in a single time step, while  $N_t$  stands for the amount of time steps with  
 170 measurements);  $\varepsilon$  denotes the observation error, with a observation error covariance matrix  
 171  $R$ ;  $B_{o,i,j}^f$  represents the vector of forecasted apparent resistivity at observation locations;  $\Delta A_j$   
 172 and  $\Delta B_j$  are square root matrices defined as

$$173 \quad \Delta A_j = \frac{1}{\sqrt{N_e - 1}} [A_{1,j} - \bar{A}_j, A_{2,j} - \bar{A}_j, \dots, A_{N_e,j} - \bar{A}_j], \quad (10)$$

$$174 \quad \Delta B_j^f = \frac{1}{\sqrt{N_e - 1}} [B_{1,j}^f - \bar{B}_j^f, B_{2,j}^f - \bar{B}_j^f, \dots, B_{N_e,j}^f - \bar{B}_j^f], \quad (11)$$

176 where  $\bar{A}_j$  and  $\bar{B}_j^f$  are the ensemble means of the CSAC parameters subject to identification  
 177 and of the forecasted apparent resistivity at the  $j_{th}$  iteration, respectively.

## 178 2. Inflation factor

179 The inflation factor  $\alpha_j$  is employed to augment the covariance matrix associated with  
 180 the measurements errors to damp the changes in the model parameters at early iterations  
 181 (Emerick and Reynolds, 2013). It is influential to the functioning of the ES-MDA, therefore,  
 182 several ways on how to compute them have been described in previous studies (Le et al., 2016;  
 183 Rafiee and Reynolds, 2017; Evensen, 2018). In this work, based on our previous experience  
 184 (Chen et al., 2022), we decide to apply the inflation factor scheme proposed by Rafiee and  
 185 Reynolds (2017). According to their detailed procedures, the first step is to generate the  
 186 initial inflation factor based on the following equation:

$$\alpha_1 = \left( \frac{1}{N} \sum_{i=1}^N \lambda_i \right)^2, \quad (12)$$

where  $\alpha_1$  denotes the initial inflation factor;  $N$  is the minimum between ensemble size  $N_e$  and the total amount of apparent resistivity measurements  $N_o \cdot N_t$ ;  $\lambda_i$  denotes the singular values of the dimensionless sensitivity matrix  $D_j$ , which is defined as

$$D_j = R^{-\frac{1}{2}} \Delta B_j^f. \quad (13)$$

Then, the succeeding inflation factors are determined in a geometrical decreasing progression,

$$\alpha_j = \beta^{j-1} \alpha_1, \quad (14)$$

where  $\beta$  denotes the common ratio that ensures the summation of the reciprocal of the inflation factors equals to one. Its value can be obtained by

$$\frac{1 - (1/\beta)^{N_a-1}}{1 - 1/\beta} = \alpha_1. \quad (15)$$

### 3. The normal-score transformation

Although ES-MDA is capable of handling non-linear models, its performance deteriorated obviously when the augmented state vector followed a non-Gaussian distribution (Zhou et al., 2014; Cao et al., 2018). To address this problem, several methods have been proposed, such as using iterative approaches, reparameterizations, Gaussian mixture models and normal-score transform (Hendricks Franssen and Kinzelbach, 2008; Zhou et al., 2011; Kumar and Srinivasan, 2019). In this paper, the normal-score transform algorithm is combined with ES-MDA to deal with non-Gaussianity. The main procedure of this method follows two steps: (i) transform the non-Gaussian augmented state vector into a marginally-Gaussian vector, and then perform ES-MDA in Gaussian space; (ii) back transform the ES-MDA

Table 1: A detailed description of the proposed data assimilation framework.

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Framework: ES-MDA with coupled models

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- Generate initial ensemble,  $A_0$  (including  $K_0, C_0$ ).
  - Choose the number of ES-MDA iterations,  $N_a$ .
  - For  $j = 1$  to  $N_a$ 
    - Set  $A_{i,j}^f = A_{i,j-1}^a$  for  $i = 1, 2, \dots, N_e$ .
    - Execute the groundwater flow and solute transport simulators for each realization.
    - Calculate  $\rho$  using (4) and (6).
    - Execute the geophysical simulator, obtain apparent resistivity  $\rho_a$ .
    - Calculate  $\alpha_j$  using (12),(13),(14) and (15).
    - Apply the normal-score transformation.
    - Update model parameters  $A_{i,j}^a$  based on (9).
    - Apply the normal-score back transformation.
  - Endfor
- 

208 updates into its original space. One more thing need to point out is that the normal-  
 209 score transform algorithm does not guarantee its higher-order moments will also follow a  
 210 multi-Gaussian distribution, however, the outcome of normal-score ES-MDA outperforms  
 211 ES-MDA for clearly non-Gaussian parameters (Jafarpour and Khodabakhshi, 2011; Kumar  
 212 and Srinivasan, 2020).

213 *2.4. Data assimilation workflow*

214 Figure 1 illustrates the details of the proposed data assimilation workflow. Using this  
 215 workflow, we are able to jointly update the non-Gaussian hydraulic conductivity and source  
 216 release history by assimilating the apparent resistivity. Note that since MODFLOW and  
 217 MT3DS are finite-difference numerical methods, while ResIPy is a finite-element method, an  
 218 extra grid refinement procedure is needed before the geophysical model is run.

### 219 3. Application

#### 220 3.1. Synthetic profile description

221 To test the proposed data assimilation framework, a benchmark case with a non-Gaussian  
222 confined aquifer and time-varying contaminant release is constructed. The contaminant  
223 movement in a two-dimensional synthetic model of  $40 \times 1 \times 20m^3$  is simulated, and then a  
224 quasi-3D geophysical model (infinite in y dimension) is used to capture the evolution in time  
225 of the pollutant concentration.

226 The profile model is discretized into 80 by 1 by 40 cells, each of which is 0.5 by 1 by 0.5 m.  
227 The model is filled with fine and coarse sand, and the detailed spatial distribution of these  
228 two materials are arranged based on a truncated Gaussian simulation (Journel and Isaaks,  
229 1984) with a threshold of 25 percentage, as shown in Figure 1. Notice that, the hydraulic  
230 conductivity values of the fine and coarse sand are generated by normal distribution algo-  
231 rithm with a mean of 0.5, 15 m/d and standard deviation of 0.06, 1 m/d, respectively. The  
232 boundary conditions are defined as follows: the left boundary is a constant head boundary of  
233 30m; the right boundary is zero-flow, except for the top four cells that are time-varying in-  
234 come flow through which the contaminant enters the aquifer; the upper and lower boundaries  
235 are impermeable. Such contamination could mimic the release from a contaminated river or  
236 irrigation canal in reality. The release pattern follows the same bimodal pulse proposed by  
237 Skaggs and Kabala (1994) and used many times later by others (Figure 1) given by:

$$C(t) = 2 \cdot \exp\left(-\frac{(t-10)^2}{35}\right) + 0.6 \cdot \exp\left(-\frac{(t-25)^2}{80}\right) + \exp\left(-\frac{(t-45)^2}{40}\right) \quad 0 \leq t \leq 100$$

238 (16)

239 For the quasi-3D geophysical model, a fine triangular mesh is generated in the zone of  
240 investigation (the profile) to compute the voltage field. Moreover, the left, right and lower  
241 boundaries of the mesh have been extended to 200 m (5 times the profile length) away  
242 from the profile to mimic the infinite boundaries, and the elements gradually increase in

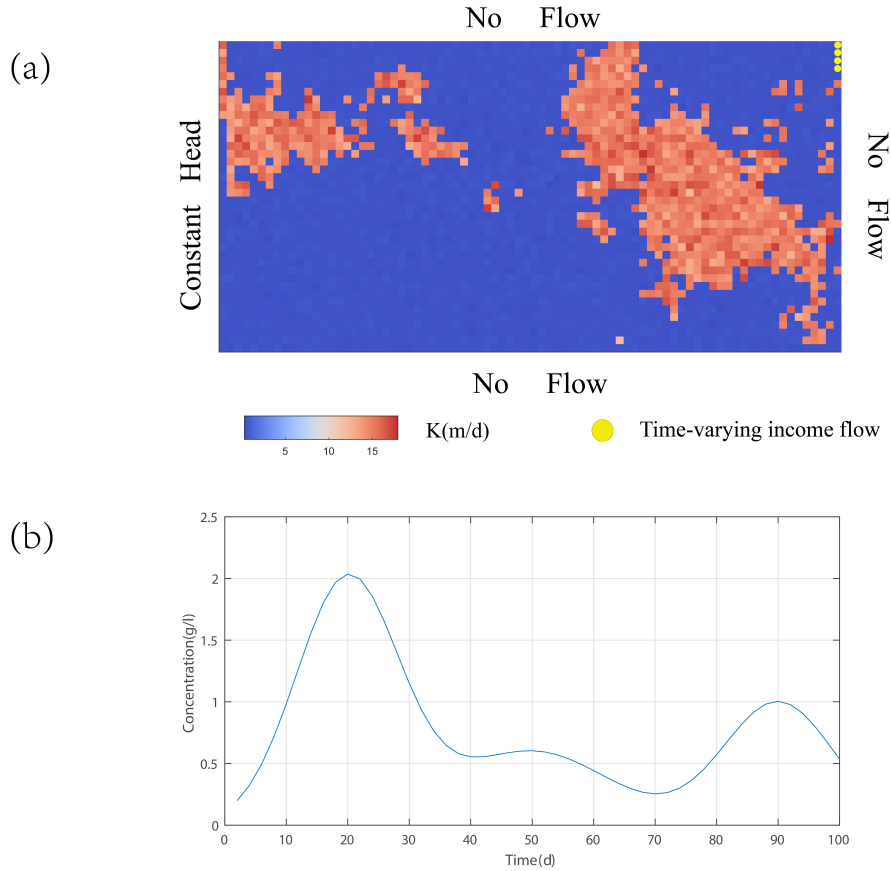


Figure 1: Schematic view of the groundwater flow and solute transport reference model. (a) Flow boundary conditions and reference hydraulic conductivity field. (b) Reference concentration release curve.

243 size laterally and vertically in this extension region. 30 electrodes are assigned in three  
 244 vertical boreholes with an interval of 2 m as shown in Figure 2. A and B denote the  
 245 current electrodes, while M and N stand for the potential electrodes. We adopt the bipole-  
 246 bipole electrode array configuration based on previous research since the cross-hole AM-BN  
 247 configuration yields greater flexibility in practice without any singularity problem in data  
 248 acquisition (Zhou and Greenhalgh, 2000). And the measurement is performed by staying  
 249 AM electrodes in one borehole and moving down the BN electrodes in the other. Once the  
 250 potential electrode N reaches the bottom of the borehole, AM electrodes will move down  
 251 one interval and then the second round of measurements get started. In this paper, the  
 252 separation between the electrodes BN is kept the same as those in AM ( $AM=BN=a$ ). Three

253 vertical separation distance values are analyzed ( $a=6$  m, 4 m, 2 m). Four different numbers  
 254 of  $\rho_a$  measurements are considered (98, 128, 162, and 388). See Table 2 for the list of  
 255 scenarios analyzed. In scenario S1, a sparse AM-BN scheme with an electrode spacing of 6  
 256 m is used (98 measurements per time step, 980 in total). This is a relatively small amount  
 257 of measurements in a time-lapse ERT survey but could happen in reality when limited data  
 258 processing capabilities are available (Binley and Kemna, 2005). We gradually increase the  
 259 number of measurements in scenarios S2 and S3, with AM-BN schemes of 128 and 162  
 260 measurements, respectively. In scenario S4, all three electrode separation distances are used,  
 261 resulting in a total of 388 measurements per time step.

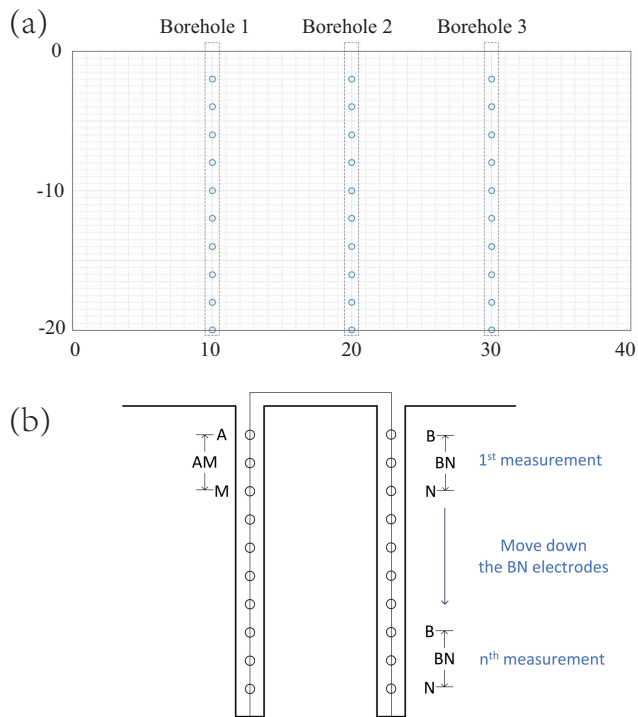


Figure 2: Schematic view of the geophysical synthetic model. (a) The distribution of the boreholes and electrodes. The black dotted box represents the borehole; the blue circle stands for a single electrode. (b) Configuration of the bipole-bipole electrodes array. A and B denote the current electrodes, while M and N stand for the potential electrodes.

262 The total simulation time of groundwater flow and transport solute is 100 days, and the  
 263 models are run in 50 equal-sized time steps. As for the geophysical model, the measurements

Table 2: Definition of the synthetic scenarios

	Scenario 1	Scenario 2	Scenario 3	Scenario 4
Vertical separation distance, $a$ (m)	6	4	2	2, 4 and 6
Number of $\rho_a$ measurements	98	128	162	388

264 are acquired with a time interval of 10 days. A more detailed description of the parameters  
 265 used in the MODFLOW, MT3DS and ResIPy models are listed in Table 3. The reference  
 266 hydraulic head, a couple of snapshots of the reference contaminant plumes and their related  
 267 reference resistivity are shown in Figure 3.

268 For the assimilation phase, and based on our previous work (Chen et al., 2018, 2021; Xu  
 269 et al., 2021), the number of iterations ( $N_a$ ) is chosen to be 4, the ensemble size ( $N_e$ ) is taken  
 270 as 500. The initial hydraulic conductivity distribution fields are generated from the same  
 271 algorithm as the reference one, while the initial release history ensemble are generated based  
 272 on uniform distribution with a range between [0.5, 1.5] g/l. In this work, a 1.20% relative  
 273 error is added to the apparent resistivity (following a Gaussian distribution with a mean of  
 274 0 and standard deviation of  $0.1 \Omega \cdot m$ ), while the aforementioned forward models errors are  
 275 neglected.

### 276 3.2. Evaluation Criterion

277 The root mean square error (RMSE) is one of the most effective criteria to evaluate the  
 278 estimation accuracy of the ensemble-based methods and has been utilized in this work:

$$279 \quad RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (A_i^{ref} - \bar{A}_i)^2}, \quad (17)$$

280 where  $n$  denotes the number of segments in which the release history curve is discretized  
 281 or the number of cells in which hydraulic conductivity must be identified,  $A_i^{ref}$  is the  $i^{th}$   
 282 component of reference CSAC parameters, while  $\bar{A}_i$  represents the ensemble mean of the  $i^{th}$   
 283 component of the updated CSAC parameters. The smaller the values for RMSE, the better

Table 3: Groundwater flow, solute transport, geophysical model parameters

Parameters	Value
<u>Model discretization</u>	
model length along $x$ (m)	40
model length along $y$ (m)	1
model height along $z$ (m)	20
grid size $\Delta x \times \Delta y \times \Delta z$ (m)	$0.5 \times 1 \times 0.5$
total simulation time (d)	100
time step length (d)	2
number of time steps	50
<u>Groundwater flow model parameters</u>	
mean of hydraulic conductivity, coarse sand (m/d)	15
mean of hydraulic conductivity, fine sand (m/d)	0.5
Std. of hydraulic conductivity, coarse sand (m/d)	1
Std. of hydraulic conductivity, fine sand (m/d)	0.06
<u>Solute transport model parameters</u>	
longitudinal dispersivity (m)	0.5
transverse dispersivity (m)	0.025
molecular diffusion coefficient	0
initial water concentration (g/l)	0.15
<u>Geophysical model parameters</u>	
porosity, coarse sand & fine sand	0.32 <sup>a</sup>
diameter, coarse sand(mm)	2
diameter, fine sand(mm)	0.25
CEC, coarse sand(C/kg)	0.72 <sup>b</sup>
CEC, fine sand(C/kg)	5.80 <sup>b</sup>
Cementation exponent, coarse sand & fine sand	2.0 <sup>a</sup>
$B(\text{m}^{-2}\text{s}^{-1}\text{V}^{-1})$	$4.1 \times 10^{-9}$ <sup>c</sup>
$\lambda(\text{m}^{-2}\text{s}^{-1}\text{V}^{-1})$	$3.46 \times 10^{-10}$ <sup>c</sup>

<sup>a</sup> Power et al. (2013).

<sup>b</sup> Revil (2013).

<sup>c</sup> Revil et al. (2018).



284 the estimation of the CSAC parameters.

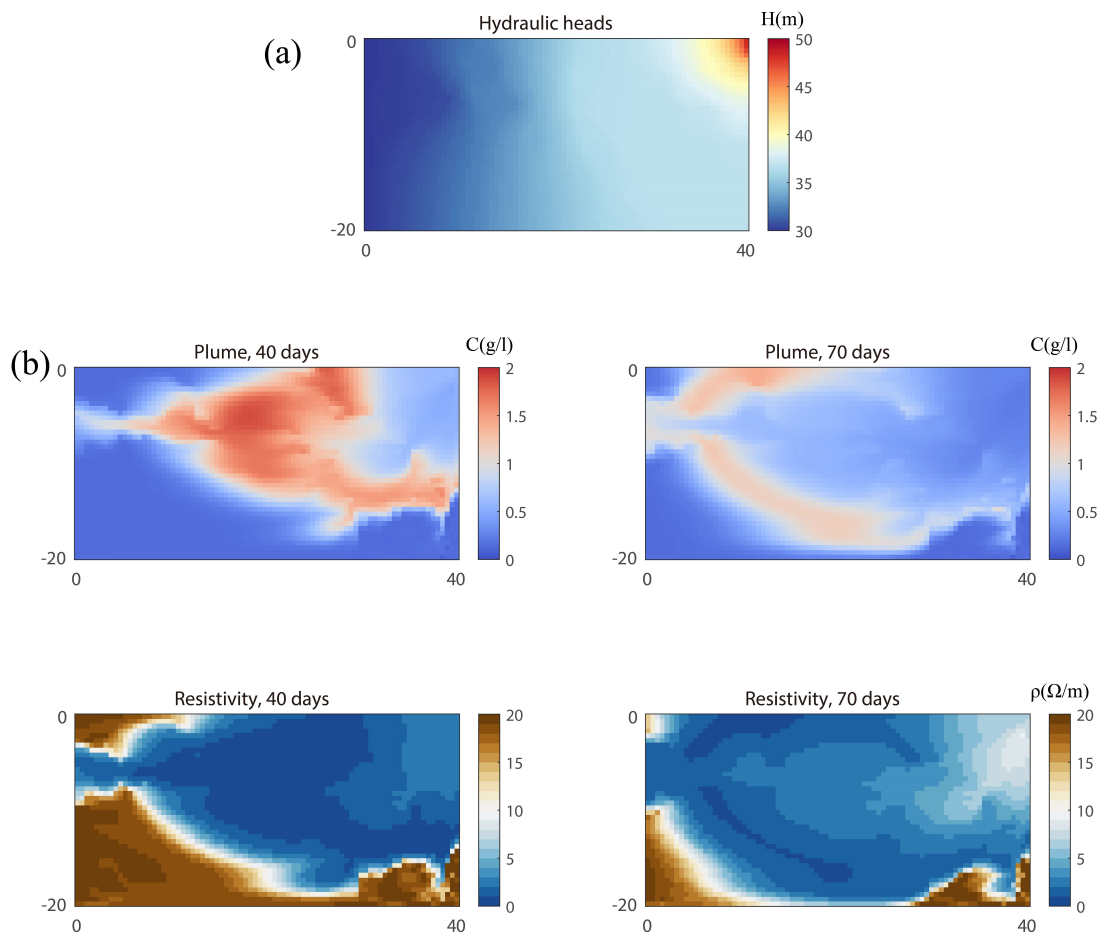


Figure 3: The properties of the reference models. (a) Hydraulic head distribution. (b) Reference contaminant plumes on day 40 and 70. (c) Reference resistivity distribution on day 40 and 70.

## 285 4. Results

### 286 4.1. Contaminant source and aquifer characterization

287 Figure 4 represents the recovered time-varying release histories for scenario S1 to S4.  
288 For each scenario, the blue dotted line illustrates the reference time-varying release history,  
289 while each gray line represents one recovered release history curve for one ensemble member,  
290 the red dotted line stands for the median, while the black dashed lines denote the 5 and 95  
291 percentiles of the recovered release history curves. It can be clearly seen that the median  
292 of the recovered release history curves follows the true release in all scenarios, but with an  
293 excess of fluctuation. This noticeable fluctuation in the ensemble medians and individual  
294 curves is believed to be caused by the inherent ill-posedness of identification problem (Chen  
295 et al., 2022). For scenarios S1 to S3, the increase in the number of measurements seems able  
296 to improve the characterization of the pollutant release curve with a narrower width of the  
297 90% confidence interval. However, in Scenario S4, with the largest number of observations  
298 with an AM-BN scheme with 388 measurements, the 90% confidence interval gets too narrow  
299 and in several instants does not contain the reference release curve. The calculated  $RMSE_c$   
300 for all scenarios is shown in Table 4 and reinforces the previous statements. For scenarios S1  
301 to S2, the  $RMSE_c$  declines slightly with the increasing of measurements, while in scenario  
302 S4, the  $RMSE_c$  has a value second only to the initial ensemble. Despite the use of an  
303 adaptive covariance inflation in this work, the ensemble variance of the release history in  
304 scenario S4 is still underestimated, and this poorly conditioned inversion can be attribute to  
305 filter inbreeding (Hendricks Franssen and Kinzelbach, 2008). Another thing to pay attention  
306 to is the bad estimation of the release curve for the last time steps. This outcome can be  
307 explained in that there are not enough data for the ES-MDA method to estimate the release  
308 at the latest release times.

309 As for aquifer characterization, Figure 5 shows the ensemble means and variances of hy-  
310 draulic conductivities for the initial ensemble and scenarios S1 to S4. The ensemble mean

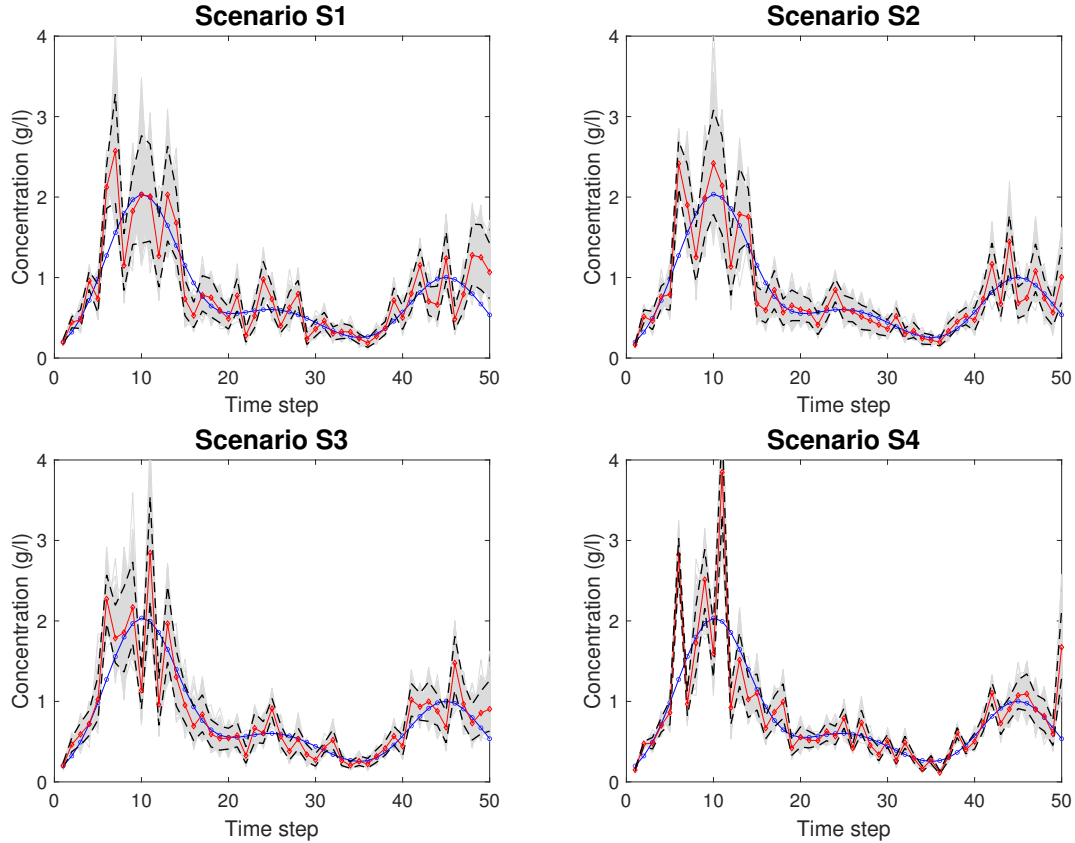


Figure 4: Recovered time-varying release histories for scenario S1-S4. The blue dotted line illustrates the reference time-varying release history, each gray line represents one recovered release history curve for one ensemble member, the red dotted line stands for the median, while the black dashed lines denote the 5 and 95 percentiles.

311 of the hydraulic conductivities in the initial ensemble is relatively homogenous, while the  
 312 ensemble variance takes a large value. After assimilating the geophysical measurements, the  
 313 ensemble mean of the updated hydraulic conductivities can delineate roughly the facies dis-  
 314 tribution in the aquifer with a substantial reduction of the ensemble variance in all scenarios.  
 315 Further comparison between all scenarios demonstrate that S2 has the best aquifer charac-  
 316 terization, with a clear identification of the high permeability area and a relatively small  
 317 ensemble variance, while S1 and S3 could delineate the high hydraulic conductivity zone less  
 318 precisely and with a larger variance. In Scenario S4, a similar outcome to S2 is obtained,  
 319 but with a poorer description of the high permeability area. A quantitative evaluation of all

Table 4: Performance of the scenario S1 to S4

	Initial ensemble	Scenario 1	Scenario 2	Scenario 3	Scenario 4
$RMSE_C$	0.535	0.3236	0.2820	0.3057	0.4416
$RMSE_K$	7.435	6.6774	6.6243	6.7221	7.0766

scenarios is listed in Table 4. Once again, we could find out that S4 has an  $RMSE_K$  value much greater than S1 to S3, this outcome is contrary to the general understanding (the more data the better the characterization). It can be the attribute to the fact that the poorly conditioned inversion of the release history in scenario S4 deteriorates the characterization of the heterogeneous hydraulic conductivities.

#### 4.2. Contaminant plume reproduction

For a more intuitive representation of the inversion results, the updated CSAC parameters are utilized to simulate the contaminant plume evolution and representative snapshots are taken to check the performance of the proposed data assimilation framework. Figure 6-9 show the reference plume, and the ensemble mean plumes simulated with the initial set of CSAC parameters and with the updated CSAC values for all 4 scenarios in days 20, 40, 70 and 90. The ensemble mean plumes generated by the initial ensemble spread widely with very large uncertainty since no observed data have been assimilated yet. The comparison between the reference and simulated contaminant plumes speaks favorably about the proposed methodology since for all 4 scenarios main contaminant plume morphology is captured at the different time snapshots. A closer look, point to S2 as the scenario that performs best, especially in the high permeability area.

Figures 10-12 show the time evolution of the vertically-averaged concentration along the boreholes 1, 2, and 3 simulated with the updated CSAC parameters for all 4 scenarios. The blue curve stands for the concentration evolution in the reference, while each gray line represents one concentration curve for one ensemble member, and the red line denotes the

341 ensemble median. The shape of the concentration curves is well reproduced in all scenarios.  
342 Again, a closer look shows that scenario S2 performs best, especially in borehole 2 and 3.

### 343 *4.3. Uncertainty evaluation for electrical properties and apparent resistivity observation error*

344 The aforementioned four scenarios (S1-S4) are carried out with two assumptions: (1) the  
345 electrical properties of fine and coarse sand (CEC values) are constant; (2) the observation  
346 error of apparent resistivity is relatively small. However, these two assumptions are somewhat  
347 idealistic. In a more realistic scenario, the uncertainties of the petrophysical properties and  
348 geophysical observations may deteriorate the performance of the proposed data assimilation  
349 framework (Troldborg et al., 2010; Laloy et al., 2012; Brunetti and Linde, 2018).

350 Hence, we have run two additional scenarios S5 and S6, which serve as repetitions of  
351 scenario S2 but with larger uncertainties in the electrical properties or apparent resistivity  
352 observation errors. More detailed, in scenario S5, the CEC values of fine and coarse sand  
353 are no longer constant, but follow a Gaussian distribution with a mean of 0.72, 5.80 and  
354 standard deviation of 0.072, 0.580 ( 10% relative error), respectively; in scenario S6, a more  
355 realistic noise (Jardani et al., 2013), which is following Gaussian distribution with a mean  
356 of 0 and standard deviation of  $1.0 \Omega \cdot m$  (12.0% relative error), is added to the apparent  
357 resistivity. The rest of the setup is exactly the same as in scenario S2, except for the electrical  
358 properties and apparent resistivity observation errors. We also show the same sets of figures  
359 shown for scenario S2. Figure 13 represents the recovered time-varying release histories for  
360 scenarios S5 and S6; Figure 14 shows the ensemble means and variances of the hydraulic  
361 conductivities for scenarios S5 and S6; Figure 16 illustrates the ensemble mean contaminant  
362 plumes computed with the updated CSAC values for scenarios S5-S6 at days 20, 40, 70 and  
363 90.

364 A quick comparison between the figures for scenarios S2 and S5 shows that the outcomes  
365 are quite similar in both scenarios. The recovered time-varying release history, ensemble

366 mean of hydraulic conductivities and the ensemble mean contaminant plumes computed  
367 with the updated CSAC values are all virtually the same in scenario S2 and S5, illustrating  
368 that the heterogeneity of electrical properties in this level hasn't deteriorate the performance  
369 of the proposed data assimilation framework. In contrast, by performing a comparative  
370 analysis of the inversion outcomes between scenarios S2 and S6, we can evaluate the effect  
371 of the observation uncertainties in the apparent resistivity. In scenario S5 , the median of  
372 the recovered release history curves has some deviations from the reference release curve  
373 (especially between time step 5 to 15) and the 90% confidence interval becomes much wider;  
374 the identified high permeability area is less accurate and the ensemble variance is still quite  
375 large; the ensemble mean plume struggles to recover the high plume concentration. In  
376 summary, we believe that both the uncertainties in the electrical properties and in the  
377 apparent resistivity observations both have some impact on our data assimilation framework,  
378 but at least in this case, the uncertainties in the apparent resistivity observations certainly  
379 deserve more attention.

380 In summary, we have again demonstrated the capacity of the proposed data assimilation  
381 framework by taking into account the uncertainties in the electrical properties and apparent  
382 resistivity observations.

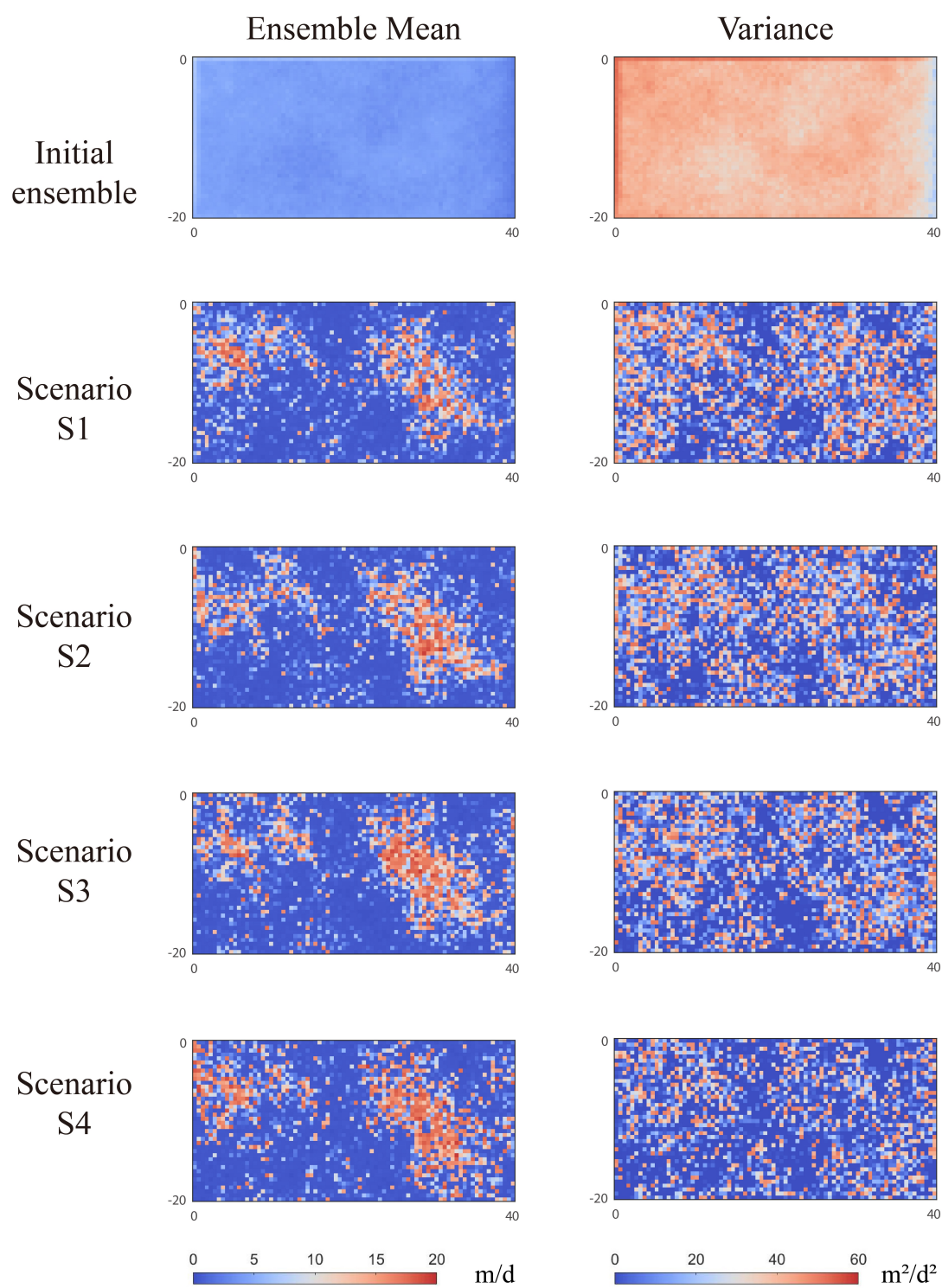


Figure 5: Ensemble means and variances of hydraulic conductivities for the initial ensemble and scenarios S1 to S4.



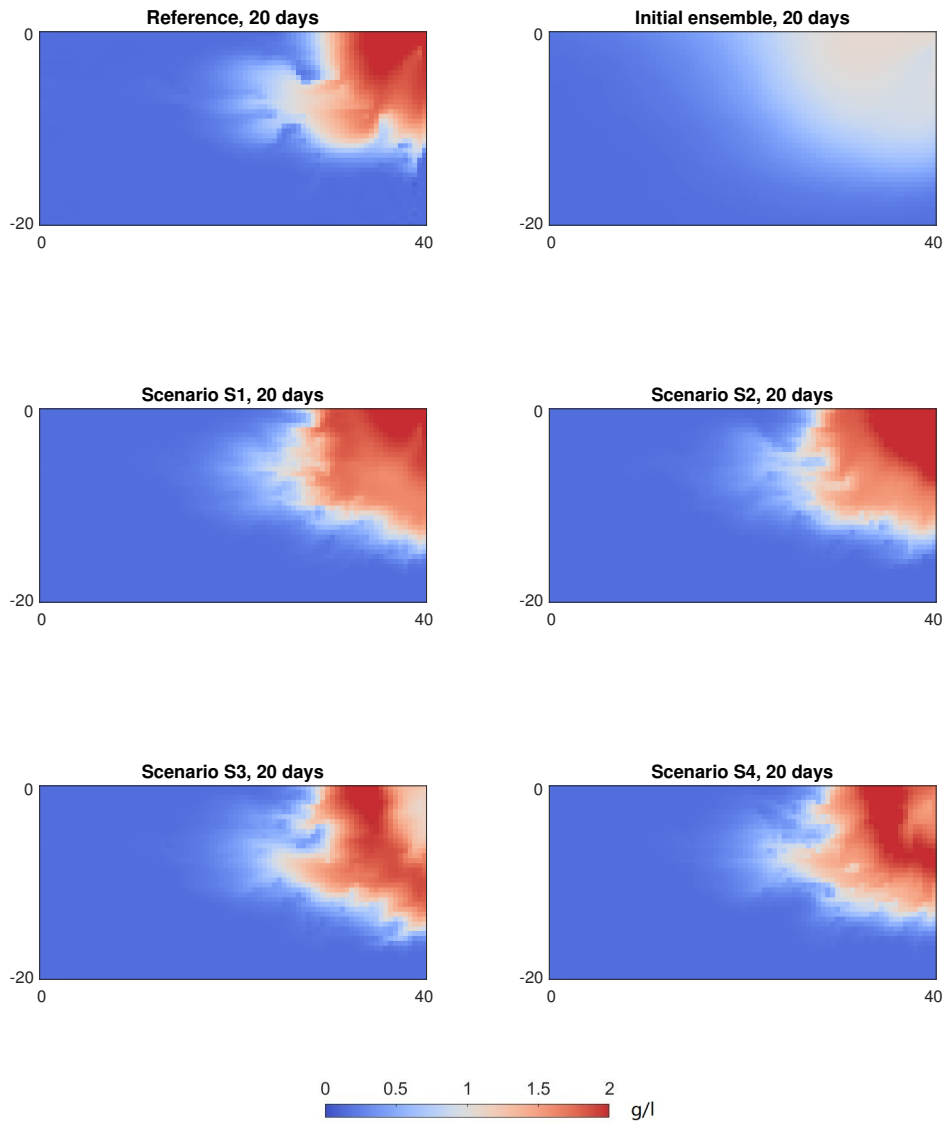


Figure 6: The reference contaminant plume and the ensemble mean contaminant plumes computed with the initial set of CSAC parameters and with the updated CSAC values for scenario S1-S4 on day 20.

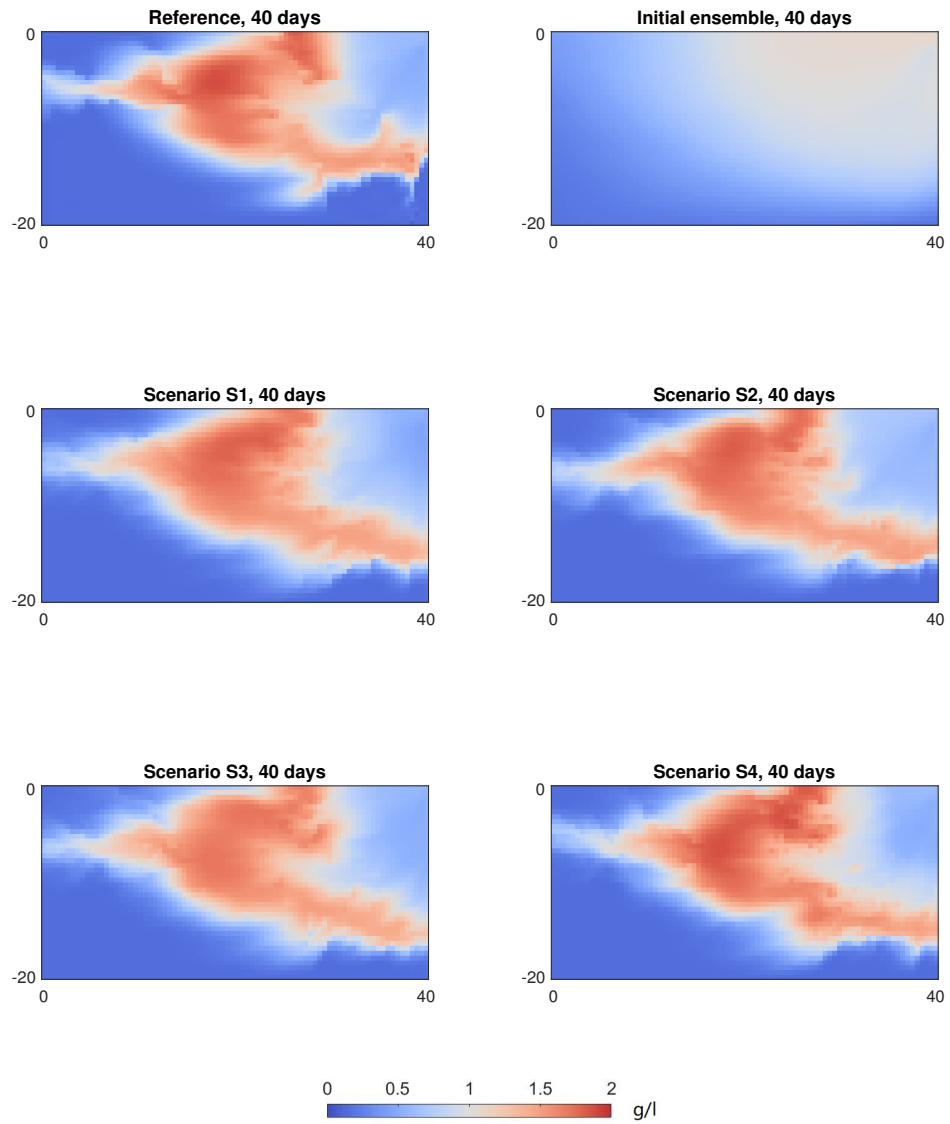


Figure 7: The reference contaminant plume and the ensemble mean contaminant plumes simulated with the initial set of CSAC parameters and with the updated CSAC values for scenario S1-S4 on day 40.

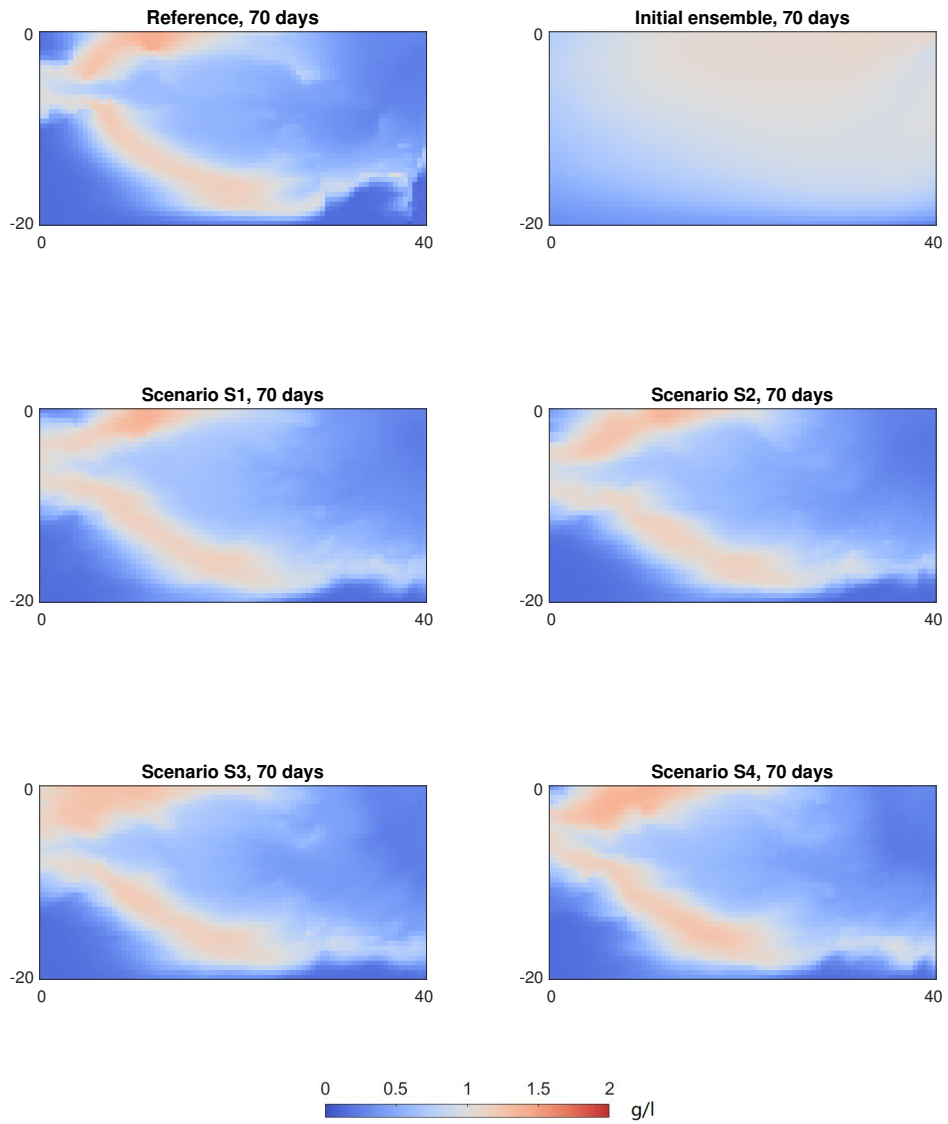


Figure 8: The reference contaminant plume and the ensemble mean contaminant plumes simulated with the initial set of CSAC parameters and with the updated CSAC values for scenario S1-S4 on day 70.

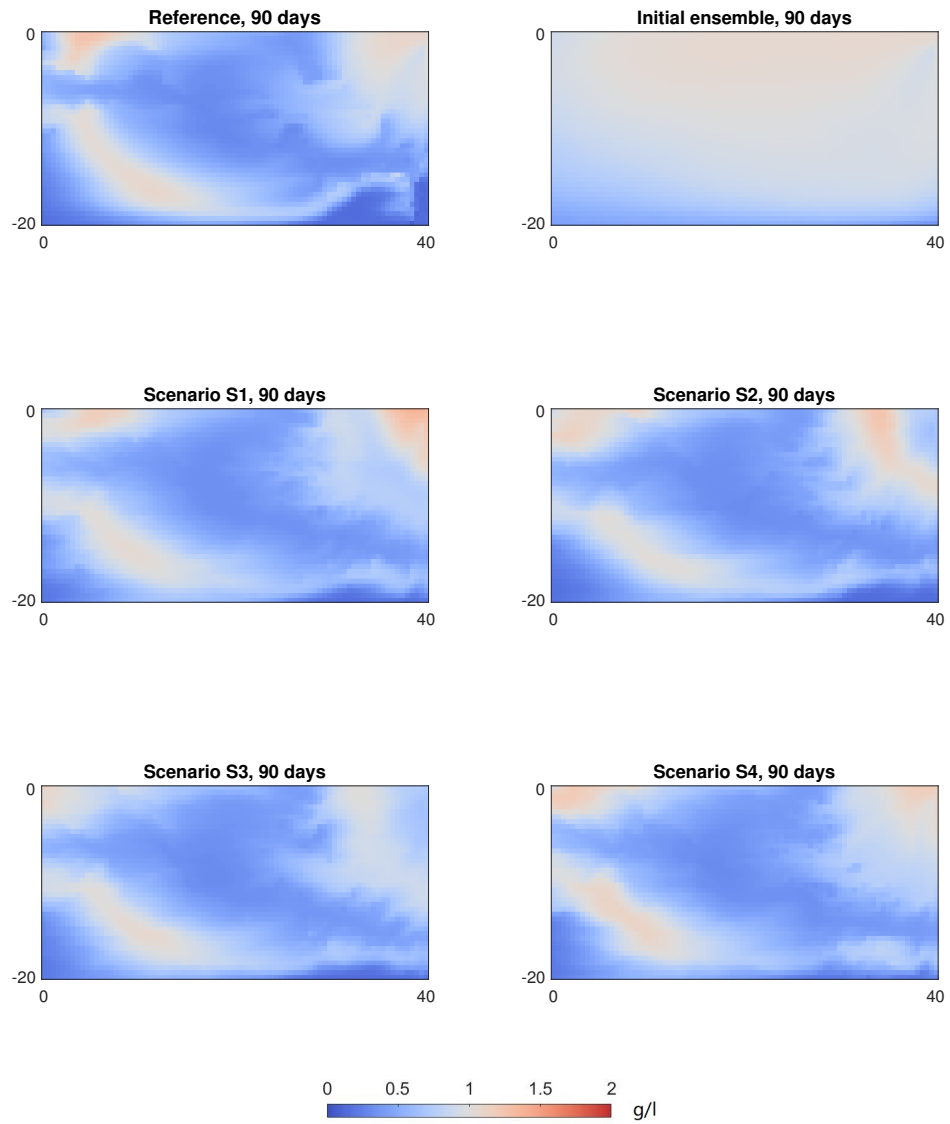


Figure 9: The reference contaminant plume and the ensemble mean contaminant plumes simulated with the initial set of CSAC parameters and with the updated CSAC values for scenario S1-S4 on day 90.

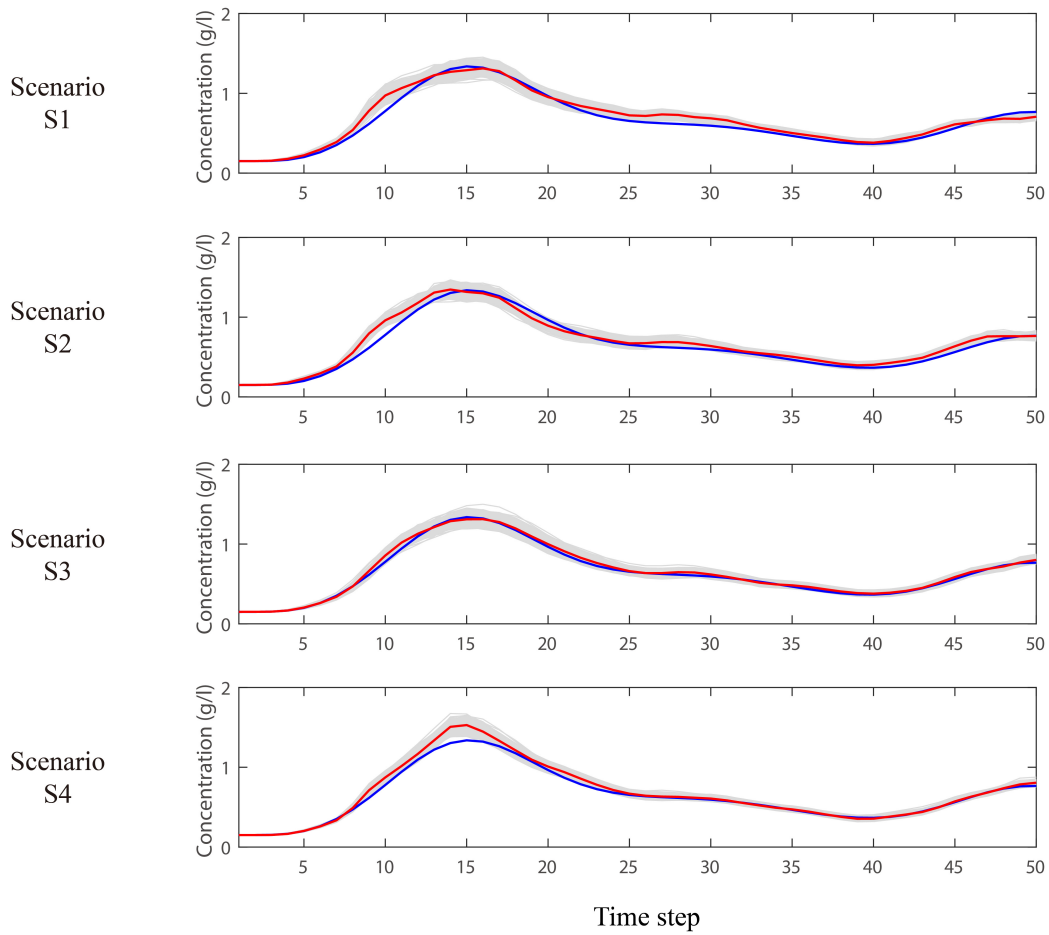


Figure 10: Time evolution of the vertically-averaged concentration of the recovered plume in borehole 1 for scenario S1-S4. The blue curve stands for the concentration evolution in the reference, while each gray line represents one concentration curve for one ensemble member, and the red line denotes the ensemble median.

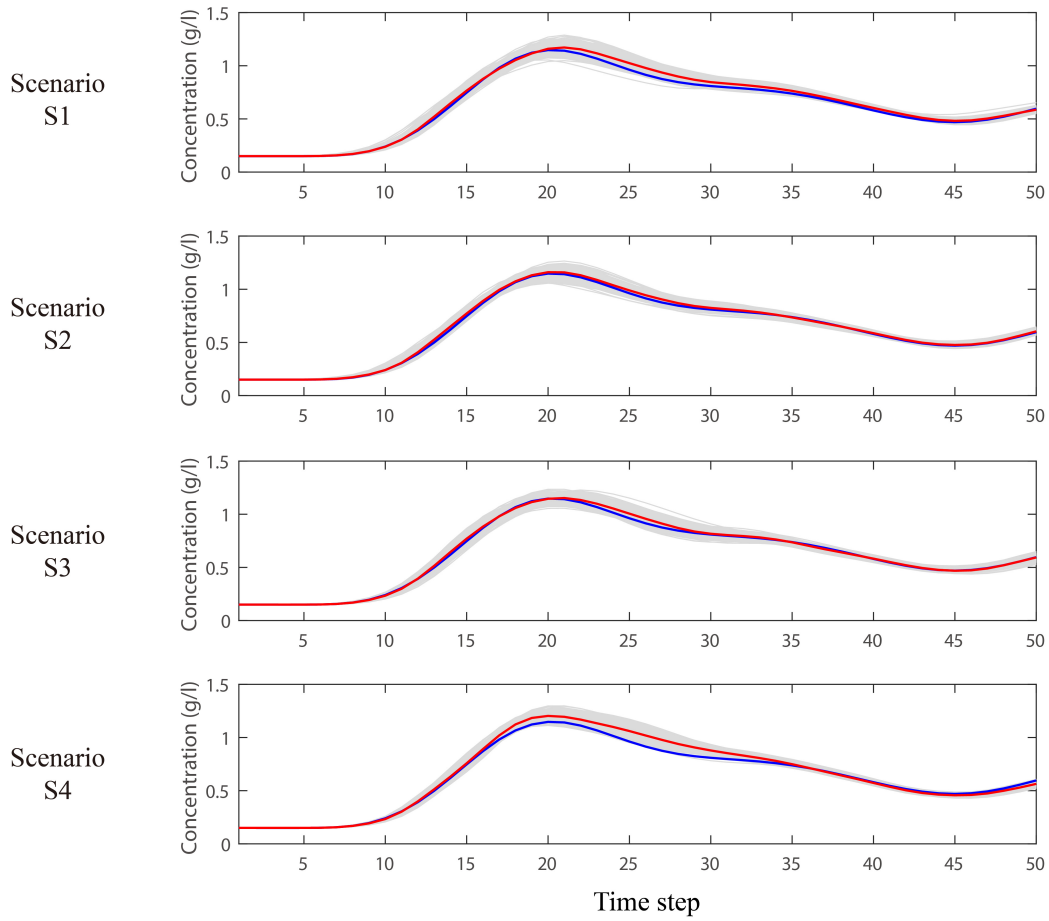


Figure 11: Time evolution of the vertically-averaged concentration of the recovered plume in borehole 2 for scenario S1-S4. The blue curve stands for the concentration evolution in the reference, while each gray line represents one concentration curve for one ensemble member, and the red line denotes the ensemble median.

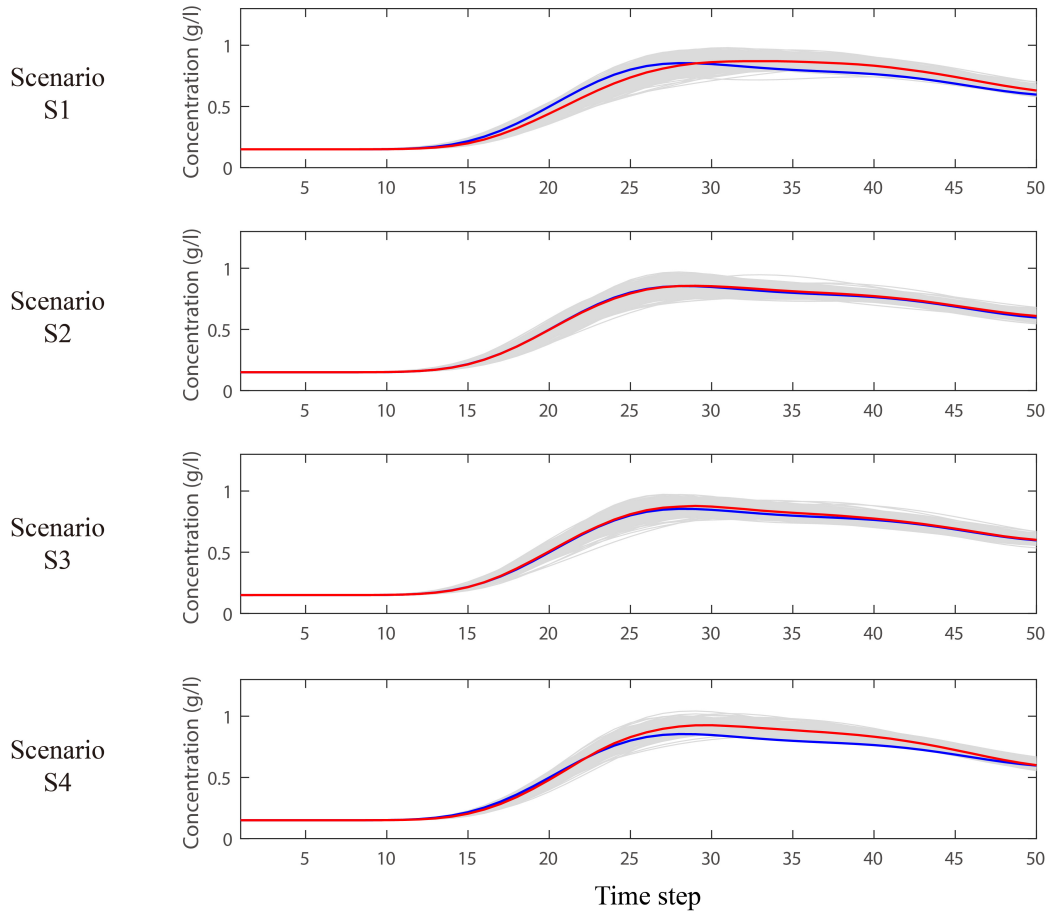


Figure 12: Time evolution of the vertically-averaged concentration of the recovered plume in borehole 3 for scenario S1-S4. The blue curve stands for the concentration evolution in the reference, while each gray line represents one concentration curve for one ensemble member, and the red line denotes the ensemble median.

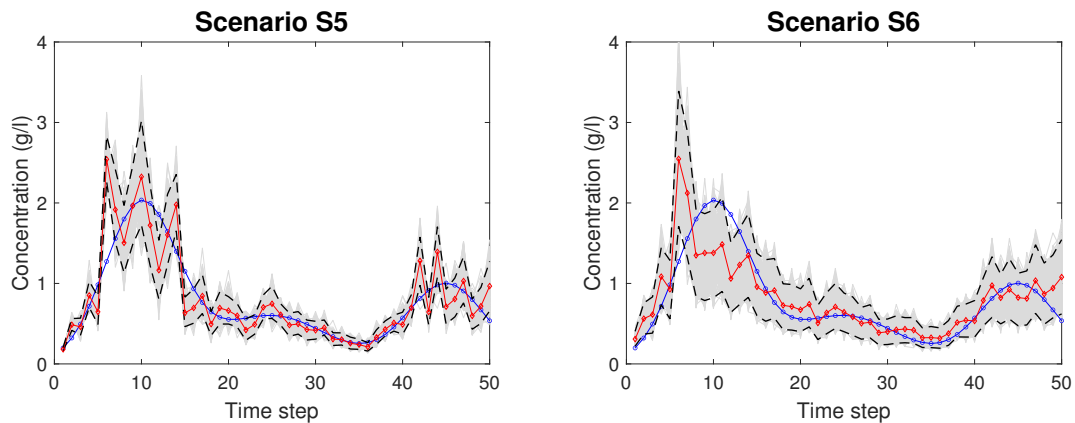


Figure 13: Recovered time-varying release histories for scenario S5-S6. The blue dotted line illustrates the reference time-varying release history, each gray line represents one recovered release history curve for one ensemble member, the red dotted line stands for the median, while the black dashed lines denote the 5 and 95 percentiles.

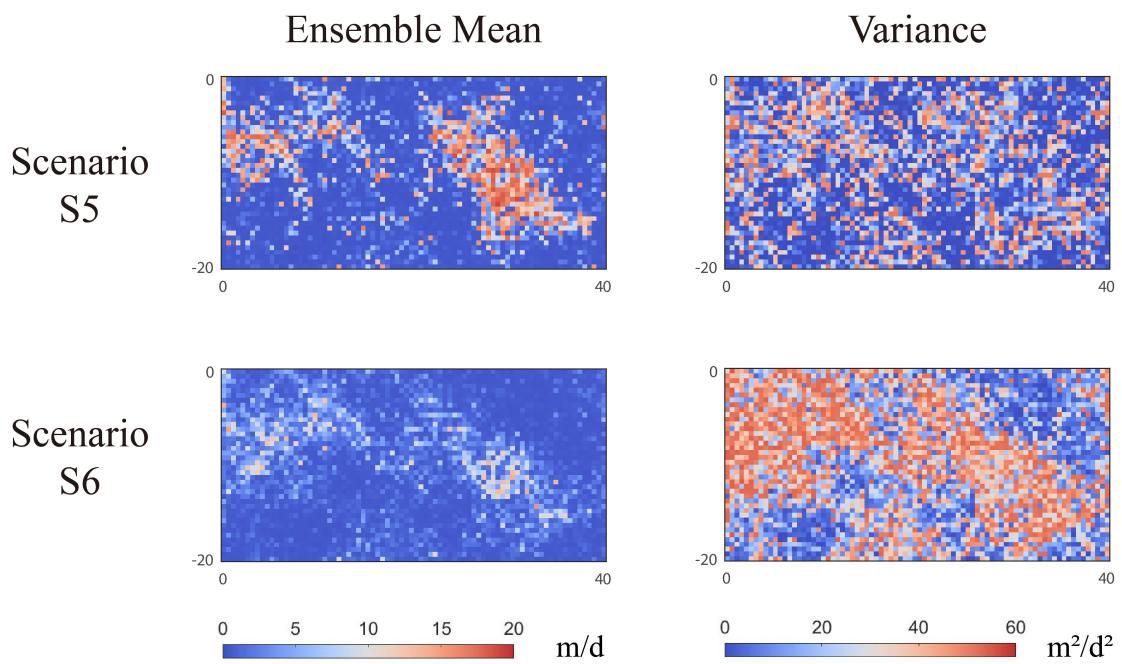


Figure 14: Ensemble means and variances of hydraulic conductivities for scenario S5-S6.



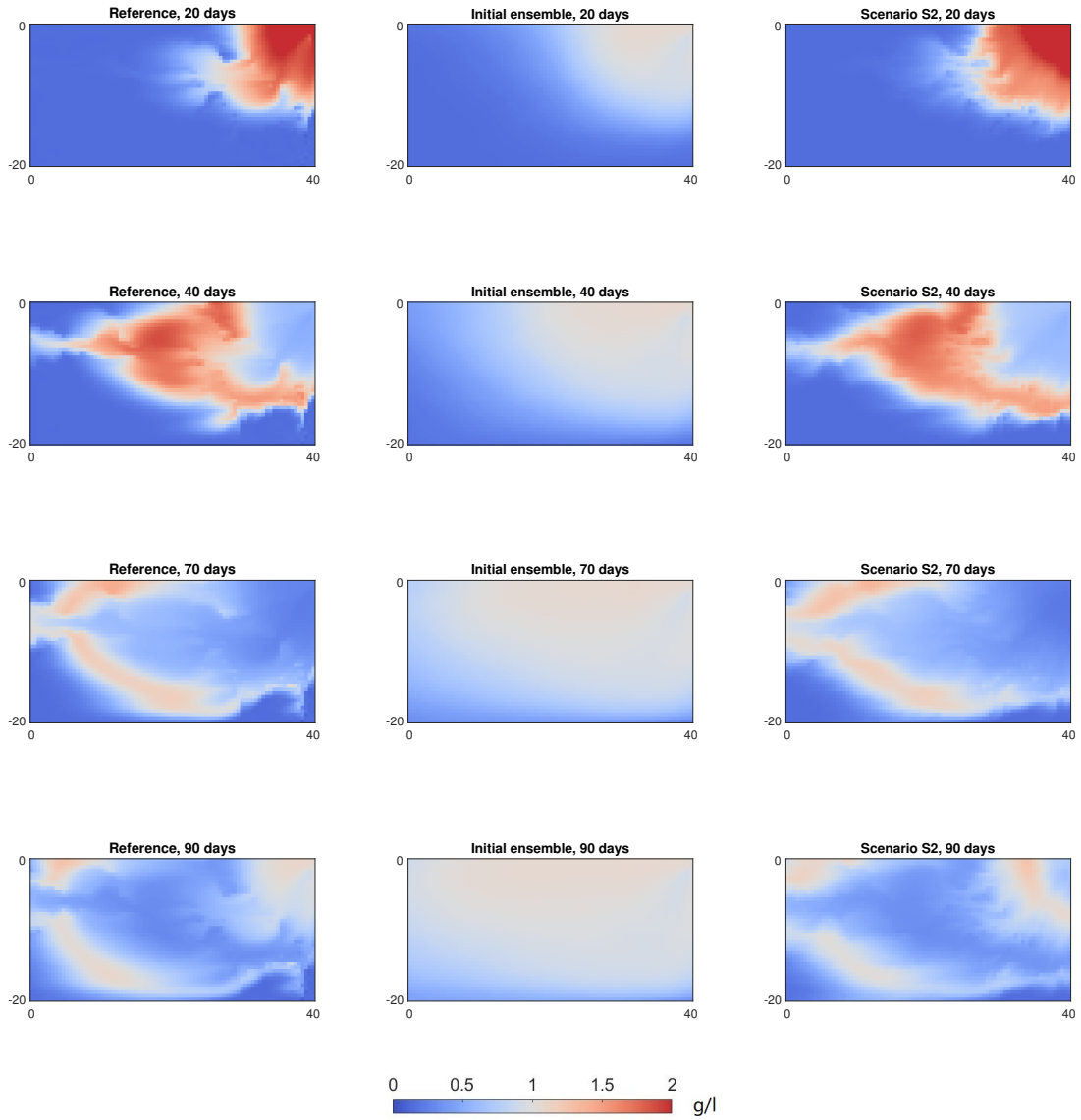


Figure 15: The ensemble mean contaminant plumes computed with the updated CSAC values for scenario S5-S6 on day 20, 40, 70 and 90.

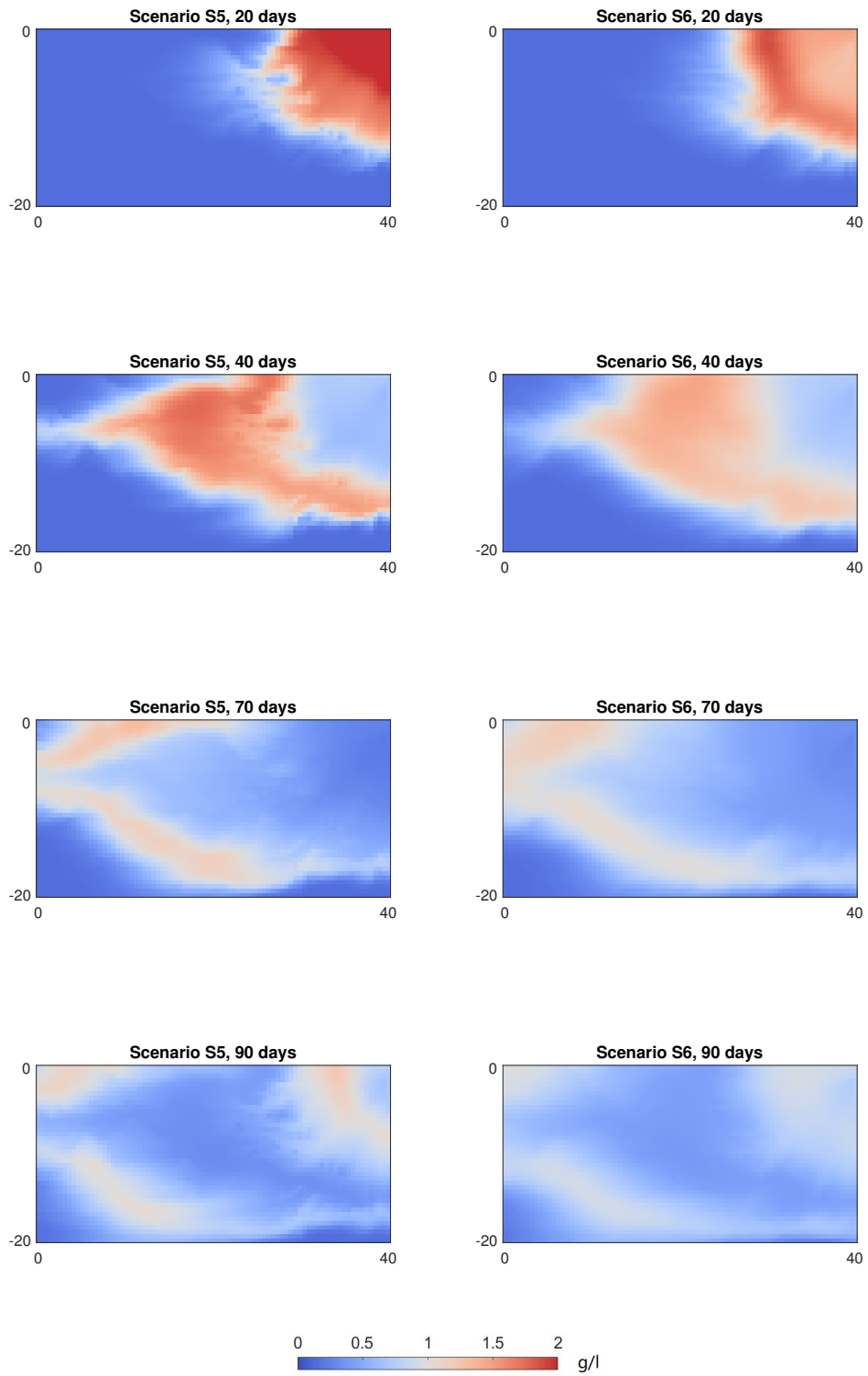


Figure 16: The ensemble mean contaminant plumes computed with the updated CSAC values for scenario S5-S6 on day 20, 40, 70 and 90.

## 383 5. Discussion

384 In this paper, we presented a performance evaluation of a proposed data assimilation  
385 framework for the groundwater contamination inverse problem in a benchmark case. The  
386 demonstration mainly presented through the following three aspects: (1) establish a coupled  
387 groundwater flow, transport solute and geophysical model; (2) build a data assimilation  
388 framework based on ES-MDA and ERT observation data; (3) joint identify contaminant  
389 source release history and hydraulic conductivities.

390 We show that the proposed data assimilation framework works well by using time-lapse  
391 ERT measurements with the proper electrode array configuration. Although the inversion  
392 of the release history may suffer from filter inbreeding, the reproduced contaminant plume  
393 via the updated CSAC parameters is still able to capture the dominant pattern of the  
394 reference contaminant plume. This result may have important implications for groundwater  
395 contamination modeling, as it suggests that an appropriate number of downstream ERT  
396 observations could help the researchers jointly identify the aquifer properties and unknown  
397 contaminant release history.

398 In this work, the electrical properties of the fine and coarse sands we used are assumed  
399 to be perfectly known. However, in field works, these parameters need to be ascertained  
400 according to dedicated field experiments before our proposed data assimilation framework is  
401 employed. While it may be argued that we have simplified the geophysical properties of the  
402 electrical model, the proposed data assimilation framework can be used as a starting point,  
403 leaving to the ES-MDA the task of evaluating the impact of uncertainties and heterogeneity  
404 around the electrical properties. In fact, this uncertainty evaluation procedure can be applied  
405 not only to the aquifer electrical properties but also to the apparent resistivity observation  
406 errors. This attribute is also indicative of the merits inherent in ensemble-based algorithms.

407 Besides, to characterize the contaminant source release history and hydraulic conductivi-  
408 ties, the difference between the background ionic concentration and the contaminant release

409 is also crucial. The temporal variation in apparent resistivity is an essential prerequisite for  
410 the proposed data assimilation framework. Hence, this data assimilation framework may  
411 suffer from larger uncertainty issues in cases with similar background ionic concentrations  
412 and contaminant releases.

413 In summary, we conclude that the proposed data assimilation framework has the capacity  
414 to identify contaminant source release history and hydraulic conductivities by using time-  
415 lapse ERT measurements with proper electrode array configuration. Moreover, it is refreshing  
416 to see that this data assimilation framework also has the capacity to handle a more complex  
417 geophysical model with large apparent resistivity observation errors.

## 418 **6. Summary and conclusion**

419 The main objective of this study is to joint identify a contaminant source release curve  
420 and hydraulic conductivities by using time-lapse ERT measurements. For this purpose,  
421 the study combines a coupled model of groundwater flow, solute transport and geophysics  
422 with the ES-MDA assimilation technique. In this data assimilation framework, only the  
423 apparent resistivity obtained from the time-lapse ERT measurements is utilized to recognize  
424 the hydraulic conductivities and contaminant release history. The proposed methodology  
425 is then validated in a synthetic benchmark with a time-varying contaminant source release  
426 in a heterogeneous aquifer. The results demonstrate that the CSAC problem could be  
427 handled by the proposed approach. The time-varying release history and the main patterns  
428 of high conductivity can be captured with proper time-lapse ERT measurements. The plume  
429 evolution computed with the updated parameters for both time-varying release curve and  
430 spatially-heterogeneous conductivity approximates well the plume computed in the reference  
431 field.

432 Besides, we also analyzed the influence of different AM-BN schemes in our data assimila-  
433 tion framework. Four scenarios with a different number of apparent resistivity measurements

434 (98, 128, 162 and 388) were designed. In scenario S4, the AM-BN scheme with a mixture of  
435 three different electrode spacing suffers from filter inbreeding producing poor results. This  
436 phenomenon can be primarily ascribed to the underestimation of ensemble variance of the  
437 release history, and needs additional attentions in further applications. We also evaluate the  
438 impact of uncertainties in the petrophysical properties and geophysical observations on our  
439 data assimilation framework, the outcomes show that the proposed ES-MDA data assimilation  
440 framework could provide convincing inversion of time-varying releasing history and  
441 hydraulic conductivities.

442 This study is significant since it is the first time that time-lapse ERT measurements are  
443 employed to identify contaminant source information together with hydraulic conductivities.  
444 And we believe this work also provides a way to assess the uncertainties from different sources  
445 when we face a more close to reality case. Insights from this work could provide a solid basis  
446 for more geophysical technologies applied in the future identification of contaminant source  
447 information and aquifer properties. But we also admit that a number of issues have not  
448 been considered, such as different electrode-array configurations, or more complex hydraulic  
449 systems. More research is needed in order to move forward and apply this approach to real  
450 problems.

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