Jointly Mapping Hydraulic Conductivity and Porosity by Assimilating Concentration Data via Ensemble Kalman Filter

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Abstract

Real-time data from on-line sensors offer the possibility to update environmental simulation models in real-time. Information from on-line sensors concerning contaminant concentrations in groundwater allow for the real-time characterization and control of a contaminant plume. In this paper it is proposed to use the CPU-efficient Ensemble Kalman Filter (EnKF) method, a data assimilation algorithm, for jointly updating the flow and transport parameters (hydraulic conductivity and porosity) and state variables (piezometric head and concentration) of a groundwater flow and contaminant transport problem. A synthetic experiment is used to demonstrate the capability of the EnKF to estimate hydraulic conductivity and porosity by assimilating dynamic head and multiple concentration data in a transient flow and transport model. In this work the worth of hydraulic conductivity, porosity, piezometric head, and concentration data is analyzed in the context of aquifer characterization and prediction uncertainty reduction. The results indicate that the characterization of the hydraulic conductivity and porosity fields is continuously improved as more data are assimilated. Also, groundwater flow and mass transport predictions are improved as more and different types of data are assimilated. The beneficial impact of accounting for multiple concentration data is patent. Key words: Data assimilation; stochastic transport; ensemble Kalman filter; multiple concentration data; hydraulic conductivity and porosity; heterogeneity

1. Introduction

- During the last several decades numerical simulation is routinely utilized to evaluate the groundwater
- 3 resources and predict the fate of contaminant plumes. The adequate characterization of spatially distributed
- hydrogeological parameters like hydraulic conductivity and porosity plays an important role in groundwater

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flow and transport simulations. However, due to the scarcity of measurements in combination with the large spatial heterogeneity it is not trivial how to characterize the spatial distribution of the mentioned parameters, and, consequently, groundwater flow and transport predictions call for an uncertainty assessment. Inverse modeling is often used to reduce model uncertainty by jointly conditioning on hard data (e.g., hydraulic conductivity and porosity) and indirect data (e.g., the observed state information, such as piezometric heads, concentrations and temperatures) to characterize the spatial variation of hydrogeological parameters. The 10 issue of how to condition on the direct measurements has been extensively investigated in the geostatistical 11 literature (e.g., Journel, 1974; Gómez-Hernández and Srivastava, 1990; Strebelle, 2002). Likewise, inverse 12 modeling, i.e., conditioning to indirect data, has been reviewed in the literature (e.g., Yeh, 1986; McLaughlin 13 and Townley, 1996; Zimmerman et al., 1998; Carrera et al., 2005; Hendricks Franssen et al., 2009). Commonly, 14 inverse methods define an objective function that includes the mismatch between calculated and observed 15 state values, as well as the perturbation of the initial parameter estimates. This objective function is 16 minimized by an optimization approach. Examples are the self-calibration method (Sahuquillo et al., 1992; Gómez-Hernández et al., 1997; Capilla et al., 1999; Wen et al., 2002; Hendricks Franssen et al., 2003), the pilot point method (Ramarao et al., 1995; LaVenue et al., 1995; Alcolea et al., 2006), the Markov chain Monte Carlo method (Oliver et al., 1997), and the gradual deformation method (Hu, 2000; Capilla and Llopis-Albert, 2009). 21

Albeit the abundant literature on inverse conditioning of conductivities to piezometric head, only a few 22 works have paid attention on jointly conditioning on head and concentration data to improve the characteri-23 zation of multiple hydrogeological parameters. Medina and Carrera (1996) extended the maximum likelihood approach (Carrera and Neuman, 1986) to condition on concentration data for a better characterization of zoned hydraulic conductivity maps. The main shortcoming of this approach is that the small-scale heterogeneity is ignored due to the estimation of hydraulic conductivity for larger zones. Hendricks Franssen et al. (1999) calibrated both hydraulic conductivity and storativity by conditioning to transient head data using the self-calibration method (Gómez-Hernández et al., 1997). More recently, Hendricks Franssen et al. (2003) further extended the self-calibration method to calibrate hydraulic conductivity by conditioning on piezometric head and concentration data. Huang et al. (2004) also employed the self-calibration method to jointly 31 identify hydraulic conductivity and sorption partitioning coefficient by conditioning on tracer breakthrough 32 data. Fu and Gómez-Hernández (2009) employed the block Markov chain Monte Carlo method to calibrate conductivity by jointly conditioning to head and travel time data. Llopis-Albert and Capilla (2009) utilized the gradual deformation method to estimate the conductivity by incorporating head, concentration and travel

time data. Schwede and Cirpka (2009) used the quasi-linear geostatistical approach of Kitanidis (1995) to
estimate conductivity by conditioning on steady-state concentration measurements. Barnhart et al. (2010)
employed PEST (Doherty, 2004), a model-independent nonlinear parameter estimation program, to calibrate
hydraulic conductivity by conditioning to concentration data collected from wireless sensor networks. These
approaches are able to generate multiple equally-likely parameter fields conditional to static and dynamic
measurements, thus capable of depicting small-scale variability of hydraulic conductivity. However, the main
shortcoming of those methods is that they are CPU-intensive; these methods require running the forward
model multiple times during the iterative optimization process of each realization.

The Ensemble Kalman Filter (EnKF) (Burgers et al., 1998; Evensen, 2003), based on the sequential
Bayesian updating rule, can be used to obtain results similar to those obtained by Monte-Carlo (MC)
type inverse methods but with reduced CPU time (see section 2.2), and it is also flexible to incorporate
multiple sources of uncertainty. Hendricks Franssen and Kinzelbach (2009) carried out a synthetic exercise
and demonstrated that EnKF needs around a factor of 80 less CPU time than the self-calibration method
to attain similar results. The EnKF can also handle data from on-line sensors that become available in
real-time and assimilate them into an on-line model. The traditional inverse methods are not well suited to
assimilate information that becomes available in real-time. EnKF provides an ensemble of updated stochastic
realizations which can be used for uncertainty analysis.

The EnKF is increasingly applied, in atmospheric sciences, land-atmosphere interaction, petroleum engineering and hydrogeology (e.g. Anderson, 2001; Reichle et al., 2002; Wen and Chen, 2005; Chen and Zhang, 2006; Nowak, 2009; Hendricks Franssen et al., 2011; Zhou et al., 2011b). In atmospheric sciences or land surface models in general only the model states are updated, whereas in petroleum engineering and hydrogeology both system parameters and state variables are commonly addressed (Naevdal et al., 2005).

The EnKF has been successfully applied to assimilate dynamic piezometric head data to improve model predictions (e.g., Chen and Zhang, 2006; Hendricks Franssen and Kinzelbach, 2008; Sun et al., 2009; Li et al., 2011c; Zhou et al., 2011a). With regard to assimilating concentration data, Huang et al. (2008) conducted a synthetic experiment and calibrated hydraulic conductivity fields by assimilating piezometric head and concentration data. In their experiment, flow was at steady-state. Liu et al. (2008) estimated multiple parameters (i.e., hydraulic conductivity, dispersivities, mobile/immobile porosities) by assimilating piezometric head and concentration data in the steady-state flow model for the MADE site. It is worth to note that they used constant values as the prior estimates for the mentioned parameters, and perturbed the parameters, by assimilating observation data via EnKF, to yield heterogeneous fields. Our aim is to

quantify the uncertainty of parameters and states starting with heterogeneous fields by conditioning on the direct measurements. Schöniger et al. (2011) assimilated normal-score transformed concentration data to calibrate hydraulic conductivities. They concluded that the improvement by the normal-score transformation (as compared with the classical EnKF, which uses untransformed data) is limited because after univariate normal transformation of the state variable, the concentration distribution is far from multi-Gaussian.

In comparison with the effort devoted to characterize the spatial variability of hydraulic conductivity by conditioning state information, less attention has been paid to identifying the spatial variability of porosity, probably due to its relatively small spatial variability ranging from 0.1 to 0.55 in unconsolidated granular aquifers (Freeze and Cherry, 1979). Additionally, various authors (e.g., Hassan, 2001; Riva et al., 2008; Hu et al., 2009; Jiang et al., 2010) have demonstrated (both in synthetic examples and real aquifers) the significance of accounting for the heterogeneity of porosity on predictions of solute movement.

We will demonstrate the capability of the EnKF to jointly map the hydraulic conductivity and porosity fields by assimilating dynamic piezometric head and multiple concentration data. Few studies have considered the conditioning with help of both multiple concentration data and dynamic piezometric head data to characterize unknown parameters. Also, to the best of our knowledge, this is the first work proposing the joint estimation of spatially distributed hydraulic conductivity and porosity fields in hydrogeology.

The remaining of this paper is organized as follows. We first summarize in section 2 the mathematical framework of the EnKF and discuss the jointly mapping of hydraulic conductivity and porosity by assimilating multiple concentration data. In section 3, a synthetic example is used to demonstrate the effectiveness of the EnKF. The paper ends with summary and conclusions in section 4.

2. Data Assimilation with the EnKF

First, the flow and transport equations (i.e, the transfer functions) will be presented, and then the algorithm of EnKF is introduced with emphasis on the assimilation of concentration data.

90 2.1. Flow and Transport Equations

The well known flow equation of an incompressible or slightly compressible fluid in saturated porous media can be expressed by combining Darcy's Law and the continuity equation (Bear, 1972; Freeze and Cherry, 1979):

$$\nabla \cdot \left(K \nabla h \right) = S \frac{\partial h}{\partial t} + W \tag{1}$$

where K is the hydraulic conductivity $[LT^{-1}]$ (which, without loss of generality, will be considered as a scalar at the characterization scale), h is the piezometric head [L]; W represents sources or sinks $[L^3T^{-1}]$; S is the specific storage coefficient $[L^{-1}]$; t is the time [T]; $\nabla \cdot = (\partial/\partial x + \partial/\partial y + \partial/\partial z)$ is the divergence operator of a vector field, and $\nabla = (\partial/\partial x, \partial/\partial y, \partial/\partial z)^T$ is the gradient operator of a scalar field.

Solute transport with linear equilibrium adsorption is governed by the following differential equation

$$\phi R \frac{\partial c}{\partial t} = \nabla (\phi \mathbf{D} \cdot \nabla c) - \nabla \mathbf{q} c \tag{2}$$

where c is solute concentration of solute in the water phase $[ML^{-3}]$; ϕ is the porosity [dimensionless]; \mathbf{D} is the local hydrodynamic dispersion coefficient tensor $[L^2T^{-1}]$, with eigenvalues associated with principal axes parallel and perpendicular to the direction of flow, defined as $D_I = \alpha_L |\mathbf{q}| + D_m$, $D_{II} = \alpha_T |\mathbf{q}| + D_m$, $D_{III} = \alpha_T |\mathbf{q}| + D_m$ (α_L and α_T are respectively the longitudinal and transverse pore-scale dispersivity; D_m is the molecular diffusion coefficient set to zero in this study, and \mathbf{q} is the Darcy velocity given by $\mathbf{q} = -K\nabla h$ [LT^{-1}]); \mathbf{R} is retardation factor expressed by $R = 1 + \rho_b K_d/\phi$ (ρ_b is the bulk density of soil; K_d is the distribution coefficient).

or 2.2. Ensemble Kalman Filter

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(Bear, 1972; Freeze and Cherry, 1979):

Extensive descriptions of EnKF and its algorithm can be found in Burgers et al. (1998) and Evensen (2003). Here, we mainly focus on the use of EnKF with updating both parameters (i.e., hydraulic conductivity and porosity) and states (i.e., piezometric head and concentration). It involves a forecast step and an analysis step, after the generation of the initial ensemble of hydraulic conductivity and porosity realizations.

• Step 1: Forecast model. The flow equation (1) or transport equation (2) is solved, i.e.,

$$\mathbf{Y}_k = f(\mathbf{X}_{k-1}, \mathbf{Y}_{k-1}),\tag{3}$$

where \mathbf{Y}_k is the state of the system (piezometric heads and/or concentration data) at time step t_k , f represents the groundwater flow and transport model (including boundary conditions, external stresses, and known parameters), and \mathbf{X}_{k-1} denotes the model parameters (hydraulic conductivity

and/or porosity) after the latests update at time t_{k-1} . Specifically, **X** and **Y** are expressed as:

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$$\begin{cases}
\operatorname{Case A} : \mathbf{X} = [\ln K]^T & \mathbf{Y} = [h]^T, & \text{if only } h \text{ data are available.} \\
\operatorname{Case B} : \mathbf{X} = [\ln K, \phi]^T & \mathbf{Y} = [c]^T, & \text{if only } c \text{ data are available.} \\
\operatorname{Case C} : \mathbf{X} = [\ln K, \phi]^T & \mathbf{Y} = [h, c]^T, & \text{if } h \text{ and } c \text{ data are available.}
\end{cases} \tag{4}$$

- Step 2: Analysis step. Using the observed dynamic piezometric head and concentration data, the model parameters are updated as follows:
 - 1. Build the joint vector Ψ_k , which includes the parameters (**X**) and the forecasted state values (**Y**). This vector can be split into as many members as there are realizations in the ensemble, with

$$\Psi_{k,j} = \begin{bmatrix} \mathbf{X} \\ \mathbf{Y} \end{bmatrix}_{k,j}, \tag{5}$$

being the j^{th} ensemble member of the augmented state vector at time t_k .

As an example, if the number of discretization blocks in the domain is N_k and we are in case C, i.e., updating both $\ln K$ and ϕ using both h and c data, the dimension of vector Ψ_k will be $4 \times N_k$.

2. The joint vector is updated, realization by realization, by assimilating the observations (\mathbf{Y}_k^{obs}) :

$$\mathbf{\Psi}_{k,j}^{a} = \mathbf{\Psi}_{k,j}^{f} + \mathbf{G}_{k} \left(\mathbf{Y}_{k,j}^{obs} + \boldsymbol{\epsilon} - \mathbf{H} \mathbf{\Psi}_{k,j}^{f} \right), \tag{6}$$

where the superscripts a and f denote analysis and forecast, respectively; ϵ is a random observation error vector; \mathbf{H} is a linear operator that interpolates the forecasted heads to the measurement locations, and, in our case, is composed of 0's and 1's since we assume that measurements are taken at block centers. Therefore, equation (6) can be expressed as:

$$\mathbf{\Psi}_{k,j}^{a} = \mathbf{\Psi}_{k,j}^{f} + \mathbf{G}_{k} \left(\mathbf{Y}_{k,j}^{obs} + \epsilon - \mathbf{Y}_{k,j}^{f} \right), \tag{7}$$

where the Kalman gain G_k is given by:

$$\mathbf{G}_k = \mathbf{P}_k^f \mathbf{H}^T \left(\mathbf{H} \mathbf{P}_k^f \mathbf{H}^T + \mathbf{R}_k \right)^{-1}, \tag{8}$$

where \mathbf{R}_k is the measurement error covariance matrix, and \mathbf{P}_k^f contains the covariances between

the different components of the state vector. \mathbf{P}_k^f can be estimated from the ensemble of forecasted results as:

$$\mathbf{P}_{k}^{f} \approx E\left[\left(\mathbf{\Psi}_{k,j}^{f} - \overline{\mathbf{\Psi}}_{k,j}^{f}\right)\left(\mathbf{\Psi}_{k,j}^{f} - \overline{\mathbf{\Psi}}_{k,j}^{f}\right)^{T}\right]$$

$$\approx \sum_{j=1}^{N_{e}} \frac{\left(\mathbf{\Psi}_{k,j}^{f} - \overline{\mathbf{\Psi}}_{k,j}^{f}\right)\left(\mathbf{\Psi}_{k,j}^{f} - \overline{\mathbf{\Psi}}_{k,j}^{f}\right)^{T}}{N_{e}},$$
(9)

where N_e is the number of realizations in the ensemble, and the overbar denotes average over the ensemble.

In the implementation of the algorithm, it is not necessary to calculate explicitly the full covariance matrix \mathbf{P}_k^f (of dimensions $(4 \times N_k) \times (4 \times N_k)$ for case C). The matrix \mathbf{H} is very sparse, and, consquently, the matrices $\mathbf{P}_k^f \mathbf{H}^T$ and $\mathbf{H} \mathbf{P}_k^f \mathbf{H}^T$ can be computed directly at a strongly reduced CPU cost.

• Step 3: Loop back. The updated states become the current states and the forecast-analysis loop is started again.

When the number of observation locations used in the assimilation step is not very large, the computational cost of calculating the covariances is limited. The main cost is related with the forward simulations for each of the stochastic realizations.

During the updating step, the forecasted state variables may have no physical meaning, e.g., negative concentrations. In our case, we remove negative values resetting them to zero. We have checked that when this may happen at locations far from the concentration plume and always with small values. This approach follows the one by Gu and Oliver (2006), who had a similar problem when dealing with water saturation in a reservoir characterization exercise.

The algorithm is implemented in the C software EnKF3D which is used in conjunction with finitedifference program MODFLOW (Harbaugh et al., 2000), to solve the confined transient flow equation (1),
and the solute transport code MT3DMS (Zheng et al., 1999). MT3DMS uses a third-order total-variationdiminishing (TVD) solution scheme, to solve the transport equation (2).

3. Synthetic Example

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In this section, a synthetic example will be presented to demonstrate the capability of the EnKF to calibrate the hydraulic conductivities and porosities by assimilating piezometric head and concentration

data. The resulting ensemble of realizations will be used also for uncertainty characterization; in a realworld case study, uncertainty may stem both from the conceptual model (e.g., the boundary conditions,
aquifer geometry) and from the parameters. Here, we only consider the uncertainty due to the heterogeneity
of hydraulic conductivity and porosity, no conceptual uncertainty is considered.

3.1. Experiment Setup

3.1.1. Reference Field

The reference conductivity and porosity fields are generated using the code GCOSIM3D (Gómez-Hernández and Journel, 1993) over a domain of 250 m × 250 m × 1 m, which is discretized into grid cells of size 5 m by 5 m by 1 m (see Figure 1A and 1C). Here, we assume that the two variables are independent of each other. The parameters of each random function are listed in Table 1. From these reference realizations nine conductivity and nine porosity data are sampled for conditioning purposes. The locations are shown in Figure 1B and 1D.

It is assumed that the sampled data have the same support as the grid cell. If the data support would be much smaller than the grid cell size, the additional problem of upscaling must be considered for generating the parameter realizations conditional to the direct measured data (e.g., Li et al., 2011a; Zhou et al., 2010; Li et al., 2011b).

The aquifer is assumed to be confined with impermeable boundaries on south and north, prescribed head values on the western boundary and constant flow rate on the eastern boundary (see Figure 2). The prescribed head value is 0 m along the western boundary. The total flow rate through the eastern boundary is -25 m³/d, distributed uniformly along the boundary. The initial head value is 0 m over the entire domain. The total simulation time is 500 days, and this period is discretized into 100 time steps following a geometric sequence of ration 1.05. Specific storage is assumed constant with a value of 0.003 m⁻¹. The simulated dynamic piezometric heads at the observation wells #1 to #9 in Figure 2 are sampled and will be used as assimilating data. The simulated heads at the wells #10 and #11 will be used as validation data.

The boundary conditions for the transport model are no-mass flux boundaries on the western, northern, and southern borders of the model. The eastern border is a specified advective mass flux boundary, acting as a line of sinks taking mass out of the aquifer (see Figure 2).

The code MODFLOW (Harbaugh et al., 2000) is used to solve the transient groundwater flow equation for the reference field and the pore velocities across the grid cell interfaces are calculated using the porosities in Figure 1C. This velocity field is used as input for solving the solute transport problem with help of the

MT3DMS code (Zheng et al., 1999). We only consider advection and dispersion as transport mechanisms with $\alpha_L = 1.0$ m and $\alpha_T = 0.1$ m. Conservative solute is uniformly placed over a line transverse to the groundwater flow at time t = 0 (see Figure 2). The source concentration is 900 ppm. To avoid the boundary effect as described by Naff et al. (1998), the contaminant source is separated 20 m from the western boundary and 50 m from the northern and southern boundaries. The plume snapshots at 300, 400 and 500 days will be used here to compare the EnKF solutions with the reference plume maps (see Figures 3A, 3C and 3E). The concentration is measured at 63 wells, uniformly distributed over the domain (see Figure 2). These measured multiple concentration data (see Figures 3B, 3D, 3F) will serve as assimilating data.

3.1.2. Scenario Studies

Six simulation scenarios are considered for which different types of measurement data are assimilated (see Table 2). Scenario 1 (S1) is an unconditional case. In Scenario 2 (S2) geostatistical simulation (Gómez-Hernández and Journel, 1993) is used in order to condition on the nine measured hydraulic conductivities and the nine porosities shown in Figures 1B and 1D, repsectively. For S1 and S2, 500 realizations of hydraulic conductivity and porosity are generated using the same random functions as for the reference fields. Flow and transport are calculated for each of the 500 $\ln K$ - ϕ realization couples, without conditioning to head or concentration data.

For scenario 3 (S3) dynamic piezometric head data are used to update the geostatistical realizations conditioned on hydraulic conductivity and porosity data of scenario S2. Piezometric head data from wells #1 to #9 are sequentially assimilated for the first 60 time steps (approximately 67.7 days).

In scenarios 4, 5 and 6 (S4, S5, S6) concentration data are assimilated by EnKF, in addition to hydraulic conductivity data and piezometric head data. S4 uses concentration data at 400 days, S5 uses concentration data at 300 and 400 days, and S6 uses concentration data at 300, 400 and 500 days.

The piezometric head and concentration data are sampled from the reference simulations without error.

However, during the assimilation process it is considered that the data might contain measurement errors

and therefore a diagonal error covariance matrix was used, with all non-zero terms equal to 0.0025 m² for

head data and 0.0025 ppm² for concentration data. We note, in practice, the errors for the heads and

concentration data would be not the same, and the observation errors would change with the time. From an

operational point of view, it is straightforward to integrate them into the assimilation procedure.

3.2. Assessment Measures

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The results for the six scenarios will be analyzed with the help of two metrics:

1. The average absolute bias (AAB) is a measure of accuracy defined as follows:

$$AAB(X) = \frac{1}{N_b} \sum_{i=1}^{N_b} \frac{1}{N_e} \sum_{r=1}^{N_e} |X_{i,r} - X_{ref,i}|$$
(10)

where X_i is, either the logconductivity $\ln K$, porosity ϕ , hydraulic head h or concentration c, at location 217 i, $X_{i,r}$ represents its value for realization r, $X_{ref,i}$ is the reference value at location i, N_b is number of 218 nodes, and N_e is the number of realizations in the ensemble (500, in this case). 210

2. The ensemble spread (AESP) represents the estimated uncertainty defined as follows:

$$AESP(X) = \left(\frac{1}{N_b} \sum_{i=1}^{N_b} \sigma_{X_i}^2\right)^{1/2},\tag{11}$$

where $\sigma_{X_i}^2$ is the ensemble variance at location *i*.

The smaller the values for AAB and AESP, the better the prediction of variable X.

3.3. Data Assimilation Results 223

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3.3.1. Hydraulic Conductivities and Porosities 224

scenarios. The ensemble mean is used to check whether the main patterns of variability of the parameter 227 are captured. In contrast to the individual realization showing distinctive patterns of high and low values, 228 the ensemble means are smoothed representations of the spatial variability of the parameters. The ensemble 229 variance illustrates how conditioning reduces the differences between the realizations. 230 In scenario 1, with no conditional data, the ensemble mean and variance of $\ln K$ and ϕ are very close to 231 the prior mean and variance. In scenario 2, using 9 conditioning hydraulic conductivities and porosities, the overall spatial patterns are captured, resulting in typical kriging maps. The ensemble variance maps show the typical bull-eye look of kriging maps, with zero variance at the sample locations and increasing variance away from them. The dynamic piezometric head data included in S3 help to capture better the main patterns of hydraulic conductivity with a further reduction of the variance. S4, S5 and S6 also include concentration 236 data for conditioning. The ensemble mean maps better delineate the main patterns of variability, and at the

Figures 4 and 5 show the ensemble mean and variance of the 500 logconductivity realizations for all

six scenarios. Figures 6 and 7 show the ensemble mean and variance of the 500 porosity realizations and

same time, unlike previous scenarios with strongly smoothed representations of ln K, also show some degree

of the small-scale variability. The characterization of the main patterns of $\ln K$ improves quite remarkable

with the conditioning of concentration data. For the scenario that uses the largest amount of conditioning data (S6), the patterns in the left upper corner of the area are identified very well, whereas this is not the case if only hydraulic conductivity, porosity and piezometric heads are used for conditioning. The role of concentration data on the characterization of porosity is also observable. The main patterns of porosity are clearer than without conditioning, and closer to the reference distribution. As expected, the ensemble variance, both for $\ln K$ and ϕ , reduces further in S6 as compared with the other scenarios.

From a more quantitative point of view, the calculated two metrics (see Table 3) lead to similar conclusions. When the measured hydraulic conductivity, porosity, piezometric head and multiple concentration 247 data are all used for conditioning (S6), the average absolute bias and the ensemble spread have the smallest 248 values. More precisely, when conditioning to $\ln K$, the $AAB(\ln K)$ decreases 14% (S2 vs. S1), if we further 249 condition to piezometric head, $AAB(\ln K)$ further decreases a 10% (S3 vs. S2), and there is an additional 250 reduction of a 7% when conditioning to concentrations (S6 vs. S3). Likewise $AESP(\ln K)$ goes down 12% 251 from S1 to S2, an additional 16% from S2 to S3 and 14% more from S3 to S6. Similar results can be observed when analyzing the evolution of $AAB(\phi)$ and $AESP(\phi)$. The $AAB(\phi)$ shows an 18% reduction as a consequence of conditioning to measured ϕ (S2 vs. S1), and 7% additional reduction related with conditioning to 254 concentration data (S6 vs. S2) and $AESP(\phi)$ shows a 15% reduction as a consequence of conditioning to 255 measured ϕ (S2 vs. S1), and 9% additional reduction related with conditioning to concentration data (S6 256 257

From these results, we can conclude that: (1) The direct measured hard data play the most important role to reduce the absolute bias of parameters; (2) The indirect measured head and concentration data reduce both the absolute bias and ensemble spread; (3) The best characterization of the aquifer in terms of $\ln K$ and ϕ is achieved by combining all the data.

262 3.3.2. Piezometric Heads Reproduction

Figure 8 shows the piezometric head evolution at well #2 and #10 for scenarios S1, S2, S3 and S6.

Recall that the piezometric head data continuously collected from well #1 to #9 are used for conditioning,
while wells #10 and #11 are for validation. Figure 8 shows that for S1 uncertainty is largest and that
the uncertainty is reduced for increasing amounts of conditioning data. For S2 the uncertainty is still
considerable, but if piezometric head data are used for conditioning (S3) the conditional well #2 has a good
head reproduction and the control well #10, also shows a large reduction of spread. The measured head
data play a critical role to reduce the uncertainty of predicted heads. The concentration data do not result
in a further improvement of the characterization of hydraulic head since the dynamic heads are already

271 reproduced very well in S3.

Table 4 shows the metrics regarding the piezometric head characterization at time t = 67.7 days (i.e., the 60th time step). The introduction of measured hydraulic conductivities attains around 27% reductions both for the AAB(h) and AESP(h). An additional 66% reduction of AAB(h) and 73% reduction of AESP(h) is achieved by conditioning to head data. The reductions of AAB(h) and AESP(h) almost can be ignored when concentration data are used for conditioning in S4, S5 and S6.

The main conclusions are: (1) of all the data, the measured piezometric head data are most informative for improving head predictions and reducing the prediction uncertainty; (2) the impact of concentration data for characterizing piezometric head is very small.

3.3.3. Concentrations Reproduction

Figure 9 to 12 show the ensemble mean and variance of 500 concentration realizations at time 300 and 500 days resulting from the transport simulation for all the six scenarios.

These ensemble mean maps of concentration for scenario 1 show that even though each realization 283 will have a non-Gaussian plume similar to those in the reference, the random location of high and low 284 concentrations makes that the ensemble mean maps of plume show a Gaussian shape. Introducing the hydraulic conductivity data (S2) rectifies the plume but still does not reproduce the reference. The ensemble 286 mean of the plume is further rectified when the conductivity, porosity and head data are jointly used for conditioning (S3). The reproduction of piezometric heads is very good in S3, but the limited improvement of the plume characterization indicates the importance of further conditioning on concentration data. The 289 results for scenarios S4 and S6 show that conditioning remarkably improves the characterization of the plume. 290 Conditioning to concentration data at t = 300 days (S4) also improves strongly the prediction for 500 days 291 (although the concentration data sampled at t = 500 days are not used for conditioning in scenario S4). 292 For scenarios S5 and S6 the additional concentration data from t = 400 and 500 days improve further the 293 characterization of the plume so that they are very close to the reference plumes. 294

The ensemble variance maps of the concentration fields show that the ensemble variance decreases away
from the barycenter of the plume and is close to zero outside of the plume. The ensemble variance of
concentration decreases continuously if more data are used for conditioning.

Table 5 shows the AAB and AESP values for the concentrations at three times. Conditioning to hydraulic conductivity and porosity data (S2) results in an average AAB reduction of 15% (compared with S1) and AESP reduces around 5%. Additional conditioning to piezometric head data (S3), results on average in an additional 5% reduction of AAB and an AESP reduction of around 7%. Further conditioning

to concentration data (S4, S5 and S6), yields prominent reduction of AAB and AESP (on average 19% and 20%, respectively).

We can see from the results: (1) concentration data is the type of data to most reduce the absolute bias and uncertainty of predicted concentration; (2) the direct measured data and indirect head data also have an important impact on the predicted concentrations; (3) when all the data are considered, the concentration fields are best characterized.

308 3.4. Reactive Transport Prediction Analysis

In this subsection, a reactive transport prediction experiment is conducted with modified flow boundary conditions using the conductivity and porosity obtained in the data assimilation exercise to further demonstrate the robustness of EnKF.

The flow and transport configurations are the same as before but the flow is at steady-state. The eastern constant flow rate boundary condition is replaced with the constant head boundary condition (h = -15 m) and the solute mass is subject to sorption. Besides advection and dispersion also sorption according to a reversible linear equilibrium isotherm is considered with $\rho_b = 1.81 \text{ g/cm}^3$ and $K_d = 0.52 \text{ cm}^3/\text{g}$ (similar to the values reported in the Borden aquifer (Mackay et al., 1986; Burr et al., 1994)). The reactive tracer is also released near the western boundary (see Figure 2) with the same total initial concentration. The plume snapshot at time t = 500 days (see Figure 13) is used to evaluate the worth of the different data.

MODFLOW and MT3DMS are employed to solve the flow equation (1) and reactive transport equation (2), respectively.

Figure 14 shows the ensemble mean and variance of predicted concentration fields at t = 500 days for the fields estimated from the scenarios S2, S3 and S6. It clearly shows that the predicted plume is close to the reference when multiple types of information are used for conditioning. Besides, the ensemble variance is the smallest for S6.

4. Conclusion

We have presented and demonstrated the Ensemble Kalman Filter, a data assimilation algorithm, to jointly estimate hydraulic conductivity and porosity by assimilating dynamic piezometric head and multiple concentration data in a hydrogeological stochastic model. Some of the attractive features of EnKF are the capability of assimilating data in real-time, CPU efficiency, ease of implementation without need of an adjoint model and the flexibility with regard to accounting for multiple sources of uncertainty jointly.

We have used a synthetic example (1) to demonstrate the potential EnKF has to condition in a CPU
efficient way to concentration data and (2) to analyze the worth of data for the characterization of aquifer
parameters and states (with a special focus on solute concentrations). We have found that the head data
have a distinctive impact to reduce the uncertainty of predicted piezometric head, but only a limited influence for improving the characterization of concentration distributions. Additional conditioning to multiple
concentration data was shown to improve strongly the predicted solute plume and also the characterization
of hydraulic conductivity and porosity.

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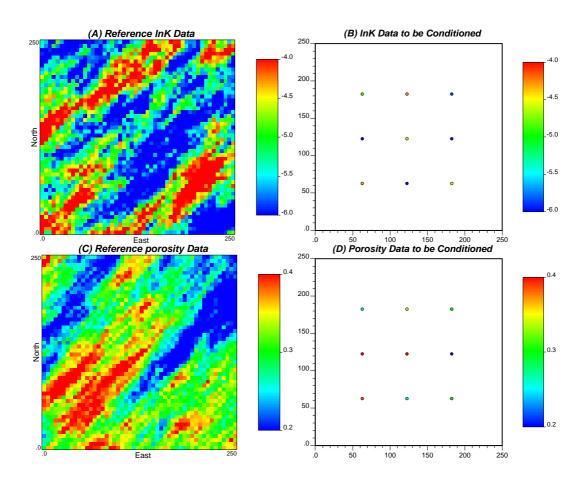


Figure 1: (A) Reference $\ln K$ field, (B) Conditioning $\ln K$ data, (C) Reference porosity(ϕ) field, (D) Conditioning porosity(ϕ) data.

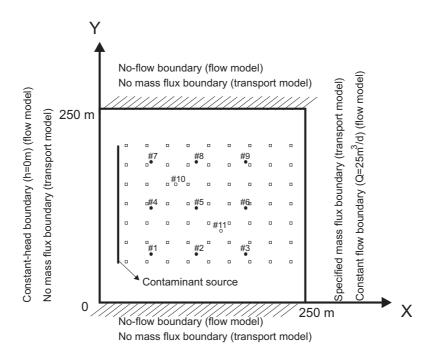


Figure 2: Sketch of the flow and transport simulation with boundary conditions and observation and prediction wells. Filled circles correspond to the pressure head observation wells (#1-#9); Open circles denote the control wells (#10-#11). Empty squares indicate the wells where concentration is sampled.

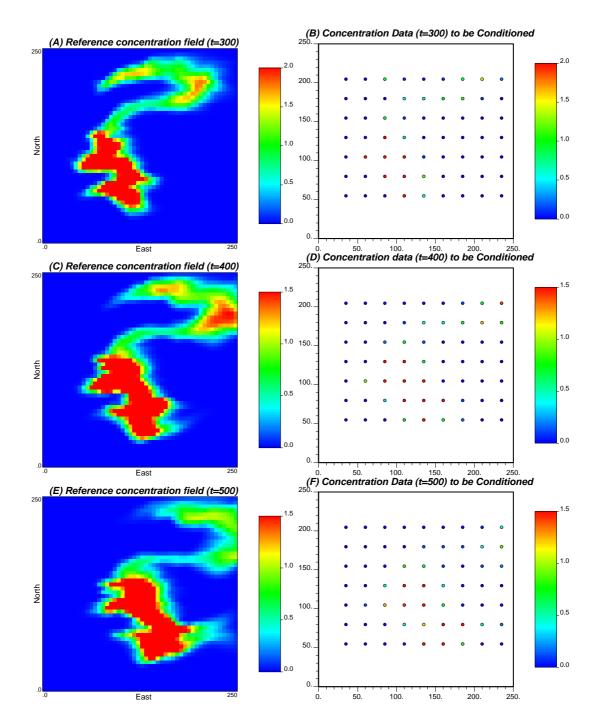


Figure 3: Reference concentration fields at time 300(A), 400(C) and 500(E) days. Conditioning concentration data at time 300(B), 400(D), and 500(F) days.

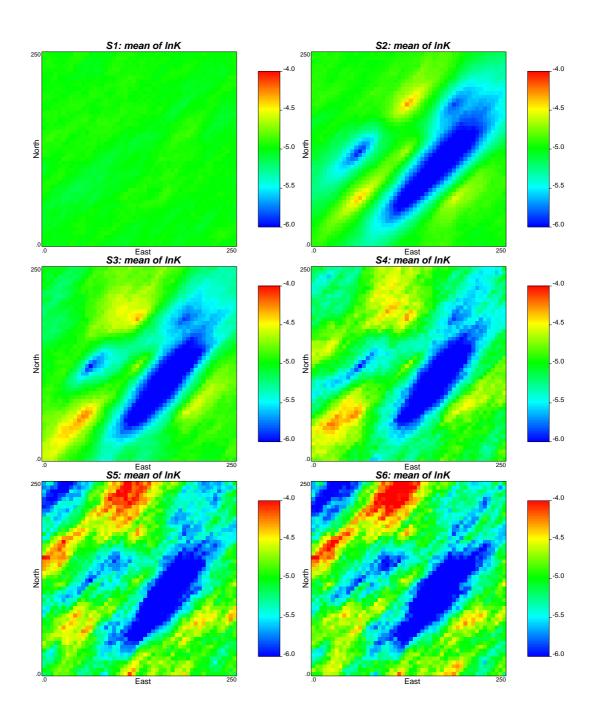


Figure 4: Ensemble average log conductivity fields for the different scenarios.

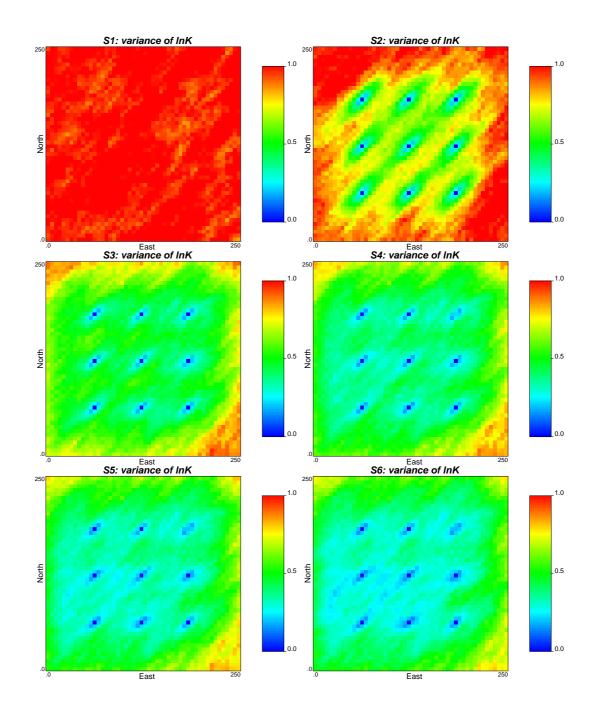


Figure 5: Ensemble logconductivity variance fields for the different scenarios $\,$

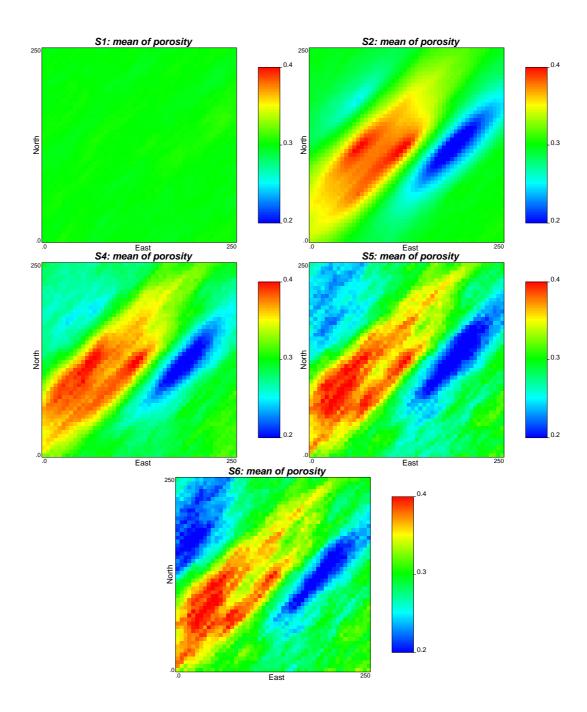


Figure 6: Ensemble average porosity fields for the different scenarios.

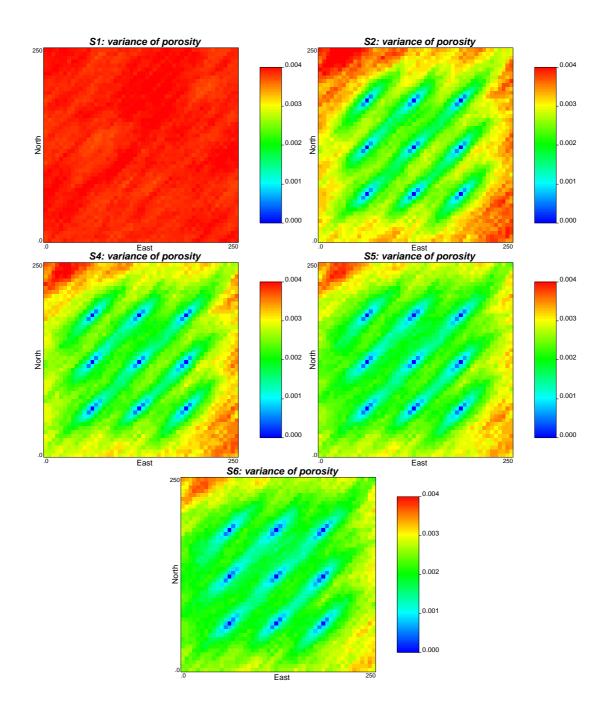


Figure 7: Ensemble porosity variance fields for the different scenarios.

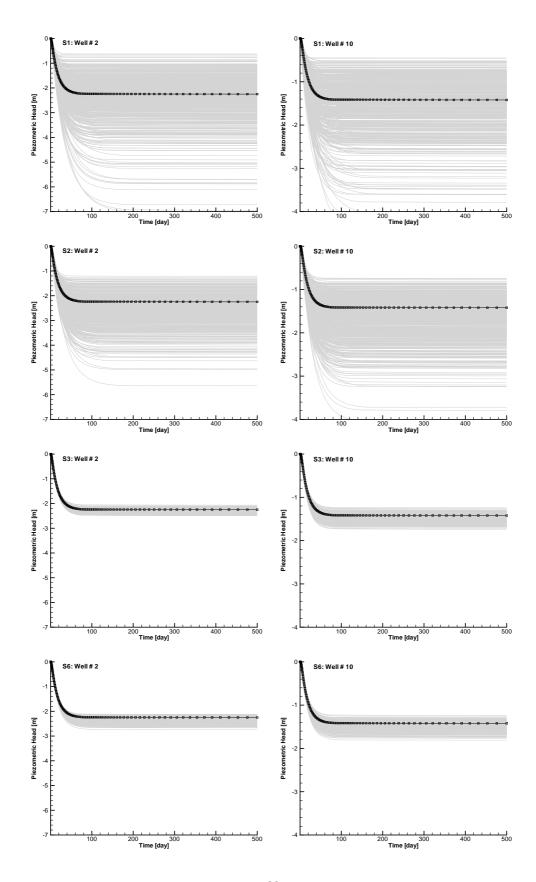


Figure 8: Piezometric head time series for the reference field ${}^{28}_{\text{Olack}}$) and simulated ones (gray lines) for the S1,S2,S3 and S6 scenarios at the conditioning well W2 (left column) and verification well W10 (right column).

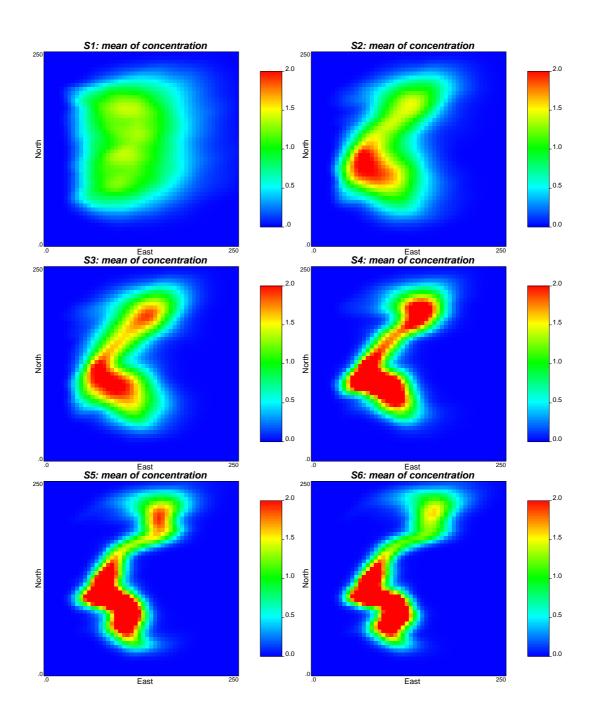


Figure 9: Ensemble average concentration fields at t=300 day for the different scenarios.

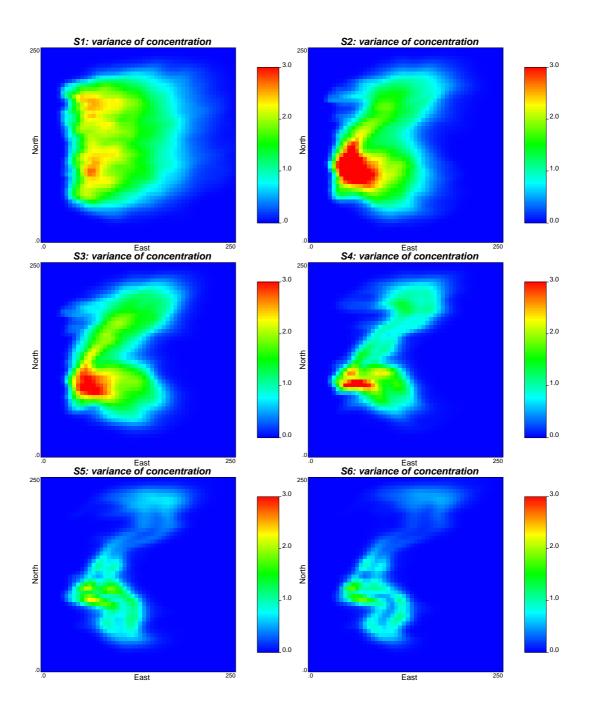


Figure 10: Ensemble variance of concentration fields at t=300 day for the different scenarios.

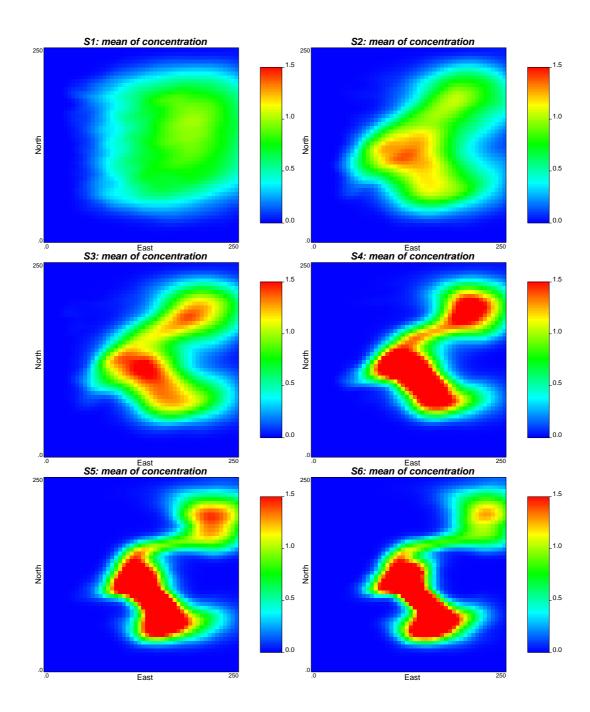


Figure 11: Ensemble average concentration fields at $t=500~\mathrm{day}$ for the different scenarios.

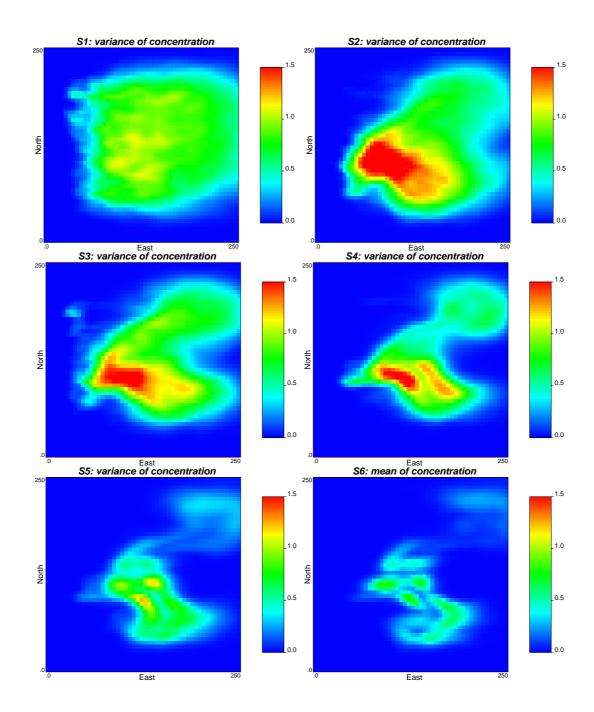


Figure 12: Ensemble variance of concentration fields at t=500 day for the different scenarios.

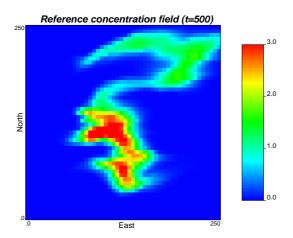


Figure 13: The reference concentration field at t = 500 days for the reactive transport prediction experiment.

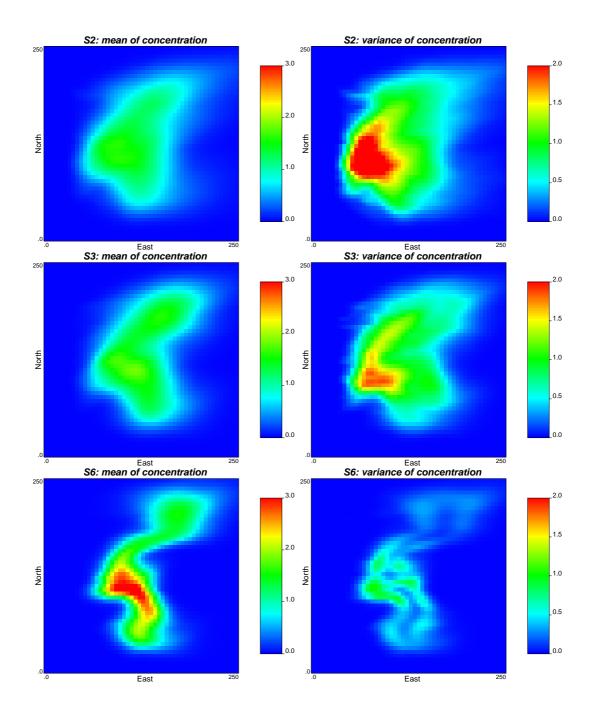


Figure 14: Ensemble mean and variance of concentration fields at t=500 day for the S2,S3 and S6.

Table 1: Parameters of the random functions for modeling the spatial distributions of $\ln K$ and porosity

	Mean	Variance	Variogram type	$\lambda_x [m]$	λ_y [m]	rotation angle β
$\ln K$	-5	1	exponential	180	60	45°
ϕ	0.3	0.0036	exponential	240	60	45°

 $[\]beta$ denotes the rotation angle of one clockwise rotation of positive y axis.

Table 2: Definition of scenarios based on the different sets of conditioning data.

Scenario	S1	S2	S3	S4	S5	S6
Hydraulic conductivities (K)	No	Yes	Yes	Yes	Yes	Yes
Porosity (ϕ)	No	Yes	Yes	Yes	Yes	Yes
Dynamic piezometric heads (h)	No	No	Yes	Yes	Yes	Yes
Concentrations $(t = 300 \text{ day})$	No	No	No	Yes	Yes	Yes
Concentrations ($t = 400 \text{ day}$)	No	No	No	No	Yes	Yes
Concentrations $(t = 500 \text{ day})$	No	No	No	No	No	Yes

Table 3: Bias and spread of $\ln K$ and porosity for the different scenarios.

Scenario	S1	S2	S3	S4	S5	S6
$AAB(\ln K)$	1.112	0.949	0.852	0.816	0.796	0.790
$AESP(\ln K)$	1.001	0.874	0.728	0.680	0.650	0.624
$AAB(\phi)$	0.072	0.059	-	0.057	0.056	0.055
$AESP(\phi)$	0.060	0.051	-	0.049	0.047	0.046

Table 4: Bias and spread of predicted piezometric heads at time t = 67.7 days for the different scenarios.

Scenario	S1	S2	S3	S4	S5	S6
$AAB(h_{t=67.7})$	0.690	0.503	0.169	0.170	0.179	0.179
$AESP(h_{t=67.7})$	0.901	0.649	0.175	0.172	0.169	0.162

Table 5: Bias and spread of predicted concentrations at time t = 300, t = 400, t = 500 days for the different scenarios.

Scenario	S1	S2	S3	S4	S5	S6
$AAB(c_{t=300})$	0.493	0.402	0.384	0.318	0.252	0.225
$AESP(c_{t=300})$	0.781	0.703	0.652	0.496	0.400	0.337
$AAB(c_{t=400})$	0.506	0.422	0.403	0.331	0.249	0.209
$AESP(c_{t=400})$	0.710	0.662	0.613	0.470	0.371	0.300
$AAB(c_{t=500})$	0.452	0.393	0.374	0.303	0.226	0.176
$AESP(c_{t=500})$	0.634	0.624	0.577	0.457	0.358	0.274